

Philosophy
of
Natural Science

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SCOPE AND AIM OF THIS BOOK

1

The different branches of scientific inquiry may be divided into two major groups: the empirical and the nonempirical sciences. The former seek to explore, to describe, to explain, and to predict the occurrences in the world we live in. Their statements, therefore, must be checked against the facts of our experience, and they are acceptable only if they are properly supported by empirical evidence. Such evidence is obtained in many different ways: by experimentation, by systematic observation, by interviews or surveys, by psychological or clinical testing, by careful examination of documents, inscriptions, coins, archeological relics, and so forth. This dependence on empirical evidence distinguishes the empirical sciences from the nonempirical disciplines of logic and pure mathematics, whose propositions are proved without essential reference to empirical findings.

The empirical sciences in turn are often divided into the natural sciences and the social sciences. The criterion for this division is much less clear than that which distinguishes empirical from nonempirical inquiry, and there is no general agreement on precisely where the dividing line is to be drawn. Usually, the natural sciences are understood to include physics, chemistry, biology, and their border areas; the social sciences are taken to comprise sociology, political science, anthropology, economics, historiography, and related disciplines. Psychology is sometimes assigned to one field, sometimes to the other, and not infrequently it is said to overlap both.

In the present series of books, the philosophy of the natural sciences and the philosophy of the social sciences are dealt with in different volumes. This separation of topics is to serve the practical purpose of

permitting a more adequate discussion of the large field of the philosophy of science; it is not intended to prejudge the question whether the division is also of systematic significance, i.e., whether the natural sciences differ fundamentally from the social sciences in subject matter, objectives, methods, or presuppositions. That there are such basic differences between those large fields has been widely asserted, and on various interesting grounds. A thorough exploration of these claims requires a close analysis of the social sciences as well as of the natural sciences and thus goes beyond the scope of this little volume. Nevertheless, our discussion will shed some light on the issue. For from time to time in our exploration of the philosophy of the natural sciences, we will have occasion to cast a comparative glance at the social sciences, and we will see that many of our findings concerning the methods and the rationale of scientific inquiry apply to the social as well as to the natural sciences. The words 'sciences' and 'scientific' will therefore often be used to refer to the entire domain of empirical science; but when clarity demands it, qualifying phrases will be added.

The high prestige that science enjoys today is no doubt attributable in large measure to the striking successes and the rapidly expanding reach of its applications. Many branches of empirical science have come to provide a basis for associated technologies, which put the results of scientific inquiry to practical use and which in turn often furnish pure or basic research with new data, new problems, and new tools for investigation.

But apart from aiding man in his search for control over his environment, science answers another, disinterested, but no less deep and persistent, urge: namely, his desire to gain ever wider knowledge and ever deeper understanding of the world in which he finds himself. In the chapters that follow, we will consider how these principal objectives of scientific inquiry are achieved. We will examine how scientific knowledge is arrived at, how it is supported, and how it changes; we will consider how science explains empirical facts, and what kind of understanding its explanations can give us; and in the course of these discussions, we will also touch upon some more general problems concerning the presuppositions and the limits of scientific inquiry, scientific knowledge, and scientific understanding.

SCIENTIFIC INQUIRY: INVENTION AND TEST

2

2.1 A case history as an example

As a simple illustration of some important aspects of scientific inquiry let us consider Semmelweis' work on childbed fever. Ignaz Semmelweis, a physician of Hungarian birth, did this work during the years from 1844 to 1848 at the Vienna General Hospital. As a member of the medical staff of the First Maternity Division in the hospital, Semmelweis was distressed to find that a large proportion of the women who were delivered of their babies in that division contracted a serious and often fatal illness known as puerperal fever or childbed fever. In 1844, as many as 260 out of 3,157 mothers in the First Division, or 8.2 per cent, died of the disease; for 1845, the death rate was 6.8 per cent, and for 1846, it was 11.4 per cent. These figures were all the more alarming because in the adjacent Second Maternity Division of the same hospital, which accommodated almost as many women as the First, the death toll from childbed fever was much lower: 2.3, 2.0, and 2.7 per cent for the same years. In a book that he wrote later on the causation and the prevention of childbed fever, Semmelweis describes his efforts to resolve the dreadful puzzle.¹

He began by considering various explanations that were current at the time; some of these he rejected out of hand as incompatible with well-established facts; others he subjected to specific tests.

¹ The story of Semmelweis' work and of the difficulties he encountered forms a fascinating page in the history of medicine. A detailed account, which includes translations and paraphrases of large portions of Semmelweis' writings, is given in W. J. Sinclair, *Semmelweis: His Life and His Doctrine* (Manchester, England: Manchester University Press, 1909). Brief quoted phrases in this chapter are taken from this work. The highlights of Semmelweis' career are recounted in the first chapter of P. de Kruif, *Men Against Death* (New York: Harcourt, Brace & World, Inc., 1932).

One widely accepted view attributed the ravages of puerperal fever to "epidemic influences", which were vaguely described as "atmospheric-cosmic-telluric changes" spreading over whole districts and causing childbed fever in women in confinement. But how, Semmelweis reasons, could such influences have plagued the First Division for years and yet spared the Second? And how could this view be reconciled with the fact that while the fever was raging in the hospital, hardly a case occurred in the city of Vienna or in its surroundings: a genuine epidemic, such as cholera, would not be so selective. Finally, Semmelweis notes that some of the women admitted to the First Division, living far from the hospital, had been overcome by labor on their way and had given birth in the street: yet despite these adverse conditions, the death rate from childbed fever among these cases of "street birth" was lower than the average for the First Division.

On another view, overcrowding was a cause of mortality in the First Division. But Semmelweis points out that in fact the crowding was heavier in the Second Division, partly as a result of the desperate efforts of patients to avoid assignment to the notorious First Division. He also rejects two similar conjectures that were current, by noting that there were no differences between the two Divisions in regard to diet or general care of the patients.

In 1846, a commission that had been appointed to investigate the matter attributed the prevalence of illness in the First Division to injuries resulting from rough examination by the medical students, all of whom received their obstetrical training in the First Division. Semmelweis notes in refutation of this view that (a) the injuries resulting naturally from the process of birth are much more extensive than those that might be caused by rough examination; (b) the midwives who received their training in the Second Division examined their patients in much the same manner but without the same ill effects; (c) when, in response to the commission's report, the number of medical students was halved and their examinations of the women were reduced to a minimum, the mortality, after a brief decline, rose to higher levels than ever before.

Various psychological explanations were attempted. One of them noted that the First Division was so arranged that a priest bearing the last sacrament to a dying woman had to pass through five wards before reaching the sickroom beyond: the appearance of the priest, preceded by an attendant ringing a bell, was held to have a terrifying and debilitating effect upon the patients in the wards and thus to make them more likely victims of childbed fever. In the Second Division, this adverse factor was absent, since the priest had direct access to the sickroom. Semmelweis decided to test this conjecture. He persuaded the priest to

come by a roundabout route and without ringing of the bell, in order to reach the sick chamber silently and unobserved. But the mortality in the First Division did not decrease.

A new idea was suggested to Semmelweis by the observation that in the First Division the women were delivered lying on their backs; in the Second Division, on their sides. Though he thought it unlikely, he decided "like a drowning man clutching at a straw", to test whether this difference in procedure was significant. He introduced the use of the lateral position in the First Division, but again, the mortality remained unaffected.

At last, early in 1847, an accident gave Semmelweis the decisive clue for his solution of the problem. A colleague of his, Kolletschka, received a puncture wound in the finger, from the scalpel of a student with whom he was performing an autopsy, and died after an agonizing illness during which he displayed the same symptoms that Semmelweis had observed in the victims of childbed fever. Although the role of microorganisms in such infections had not yet been recognized at the time, Semmelweis realized that "cadaveric matter" which the student's scalpel had introduced into Kolletschka's blood stream had caused his colleague's fatal illness. And the similarities between the course of Kolletschka's disease and that of the women in his clinic led Semmelweis to the conclusion that his patients had died of the same kind of blood poisoning: he, his colleagues, and the medical students had been the carriers of the infectious material, for he and his associates used to come to the wards directly from performing dissections in the autopsy room, and examine the women in labor after only superficially washing their hands, which often retained a characteristic foul odor.

Again, Semmelweis put his idea to a test. He reasoned that if he were right, then childbed fever could be prevented by chemically destroying the infectious material adhering to the hands. He therefore issued an order requiring all medical students to wash their hands in a solution of chlorinated lime before making an examination. The mortality from childbed fever promptly began to decrease, and for the year 1848 it fell to 1.27 per cent in the First Division, compared to 1.33 in the Second.

In further support of his idea, or of his *hypothesis*, as we will also say, Semmelweis notes that it accounts for the fact that the mortality in the Second Division consistently was so much lower: the patients there were attended by midwives, whose training did not include anatomical instruction by dissection of cadavers.

The hypothesis also explained the lower mortality among "street births": women who arrived with babies in arms were rarely examined after admission and thus had a better chance of escaping infection.

Similarly, the hypothesis accounted for the fact that the victims of childbed fever among the newborn babies were all among those whose mothers had contracted the disease during labor; for then the infection could be transmitted to the baby before birth, through the common bloodstream of mother and child, whereas this was impossible when the mother remained healthy.

Further clinical experiences soon led Semmelweis to broaden his hypothesis. On one occasion, for example, he and his associates, having carefully disinfected their hands, examined first a woman in labor who was suffering from a festering cervical cancer; then they proceeded to examine twelve other women in the same room, after only routine washing without renewed disinfection. Eleven of the twelve patients died of puerperal fever. Semmelweis concluded that childbed fever can be caused not only by cadaveric material, but also by "putrid matter derived from living organisms."

2.2 Basic steps in testing a hypothesis

We have seen how, in his search for the cause of childbed fever, Semmelweis examined various hypotheses that had been suggested as possible answers. How such hypotheses are arrived at in the first place is an intriguing question which we will consider later. First, however, let us examine how a hypothesis, once proposed, is tested.

Sometimes, the procedure is quite direct. Consider the conjectures that differences in crowding, or in diet, or in general care account for the difference in mortality between the two divisions. As Semmelweis points out, these conflict with readily observable facts. There are no such differences between the divisions; the hypotheses are therefore rejected as false.

But usually the test will be less simple and straightforward. Take the hypothesis attributing the high mortality in the First Division to the dread evoked by the appearance of the priest with his attendant. The intensity of that dread, and especially its effect upon childbed fever, are not as directly ascertainable as are differences in crowding or in diet, and Semmelweis uses an indirect method of testing. He asks himself: Are there any readily observable effects that should occur if the hypothesis were true? And he reasons: If the hypothesis were true, then an appropriate change in the priest's procedure should be followed by a decline in fatalities. He checks this implication by a simple experiment and finds it false, and he therefore rejects the hypothesis.

Similarly, to test his conjecture about the position of the women during delivery, he reasons: If this conjecture should be true, then adoption of the lateral position in the First Division will reduce the mortality. Again, the implication is shown false by his experiment, and the conjecture is discarded.

In the last two cases, the test is based on an argument to the effect that if the contemplated hypothesis, say *H*, is true, then certain observable events (e.g., decline in mortality) should occur under specified circumstances (e.g., if the priest refrains from walking through the wards, or if the women are delivered in lateral position); or briefly, if *H* is true, then so is *I*, where *I* is a statement describing the observable occurrences to be expected. For convenience, let us say that *I* is inferred from, or implied by, *H*; and let us call *I* a *test implication of the hypothesis H*. (We will later give a more accurate description of the relation between *I* and *H*.)

In our last two examples, experiments show the test implication to be false, and the hypothesis is accordingly rejected. The reasoning that leads to the rejection may be schematized as follows:

If *H* is true, then so is *I*.

2a] But (as the evidence shows) *I* is not true.

H is not true.

Any argument of this form, called *modus tollens* in logic,² is deductively valid; that is, if its premisses (the sentences above the horizontal line) are true, then its conclusion (the sentence below the horizontal line) is unfailingly true as well. Hence, if the premisses of (2a) are properly established, the hypothesis *H* that is being tested must indeed be rejected.

Next, let us consider the case where observation or experiment bears out the test implication *I*. From his hypothesis that childbed fever is blood poisoning produced by cadaveric matter, Semmelweis infers that suitable antiseptic measures will reduce fatalities from the disease. This time, experiment shows the test implication to be true. But this favorable outcome does not conclusively prove the hypothesis true, for the underlying argument would have the form

If *H* is true, then so is *I*.

2b] (As the evidence shows) *I* is true.

H is true.

And this mode of reasoning, which is referred to as the *fallacy of affirming the consequent*, is deductively invalid, that is, its conclusion may be false even if its premisses are true.³ This is in fact illustrated by Semmelweis' own experience. The initial version of his account of childbed fever as a form of blood poisoning presented infection with cadaveric matter essentially as the one and only source of the disease; and he was right in reasoning that if this hypothesis should be true, then destruction

² For details, see another volume in this series: W. Salmon, *Logic*, pp. 24-25.

³ See Salmon, *Logic*, pp. 27-29.

of cadaveric particles by antiseptic washing should reduce the mortality. Furthermore, his experiment did show the test implication to be true. Hence, in this case, the premisses of (2b) were both true. Yet, his hypothesis was false, for as he later discovered, putrid material¹ from living organisms, too, could produce childbed fever.

Thus, the favorable outcome of a test, i.e., the fact that a test implication inferred from a hypothesis is found to be true, does not prove the hypothesis to be true. Even if many implications of a hypothesis have been borne out by careful tests, the hypothesis may still be false. The following argument still commits the fallacy of affirming the consequent:

If H is true, then so are I_1, I_2, \dots, I_n .

2c] (As the evidence shows) I_1, I_2, \dots, I_n are all true.

H is true.

This, too, can be illustrated by reference to Semmelweis' final hypothesis in its first version. As we noted earlier, his hypothesis also yields the test implications that among cases of street births admitted to the First Division, mortality from puerperal fever should be below the average for the Division, and that infants of mothers who escape the illness do not contract childbed fever; and these implications, too, were borne out by the evidence — even though the first version of the final hypothesis was false.

But the observation that a favorable outcome of however many tests does not afford conclusive proof for a hypothesis should not lead us to think that if we have subjected a hypothesis to a number of tests and all of them have had a favorable outcome, we are no better off than if we had not tested the hypothesis at all. For each of our tests might conceivably have had an unfavorable outcome and might have led to the rejection of the hypothesis. A set of favorable results obtained by testing different test implications, I_1, I_2, \dots, I_n , of a hypothesis, shows that as far as these particular implications are concerned, the hypothesis has been borne out; and while this result does not afford a complete proof of the hypothesis, it provides at least some support, some partial corroboration or confirmation for it. The extent of this support will depend on various aspects of the hypothesis and of the test data. These will be examined in Chapter 4.

Let us now consider another example,⁴ which will also bring to our attention some further aspects of scientific inquiry.

⁴ The reader will find a fuller account of this example in Chap. 4 of J. B. Conant's fascinating book, *Science and Common Sense* (New Haven: Yale University Press, 1951). A letter by Torricelli setting forth his hypothesis and his test of it, and an eyewitness report on the Puy-de-Dôme experiment are reprinted in W. F. Magie, *A Source Book in Physics* (Cambridge: Harvard University Press, 1963), pp. 70-75.

As was known at Galileo's time, and probably much earlier, a simple suction pump, which draws water from a well by means of a piston that can be raised in the pump barrel, will lift water no higher than about 34 feet above the surface of the well. Galileo was intrigued by this limitation and suggested an explanation for it, which was, however, unsound. After Galileo's death, his pupil Torricelli advanced a new answer. He argued that the earth is surrounded by a sea of air, which, by reason of its weight exerts pressure upon the surface below, and that this pressure upon the surface of the well forces water up the pump barrel when the piston is raised. The maximum length of 34 feet for the water column in the barrel thus reflects simply the total pressure of the atmosphere upon the surface of the well.

It is evidently impossible to determine by direct inspection or observation whether this account is correct, and Torricelli tested it indirectly. He reasoned that if his conjecture were true, then the pressure of the atmosphere should also be capable of supporting a proportionately shorter column of mercury; indeed, since the specific gravity of mercury is about 14 times that of water, the length of the mercury column should be about $34/14$ feet, or slightly less than $2\frac{1}{2}$ feet. He checked this test implication by means of an ingeniously simple device, which was, in effect, the mercury barometer. The well of water is replaced by an open vessel containing mercury; the barrel of the suction pump is replaced by a glass tube sealed off at one end. The tube is completely filled with mercury and closed by placing the thumb tightly over the open end. It is then inverted, the open end is submerged in the mercury well, and the thumb is withdrawn; whereupon the mercury column in the tube drops until its length is about 30 inches—just as predicted by Torricelli's hypothesis.

A further test implication of that hypothesis was noted by Pascal, who reasoned that if the mercury in Torricelli's barometer is counterbalanced by the pressure of the air above the open mercury well, then its length should decrease with increasing altitude, since the weight of the air overhead becomes smaller. At Pascal's request, this implication was checked by his brother-in-law, Périer, who measured the length of the mercury column in the Torricelli barometer at the foot of the Puy-de-Dôme, a mountain some 4,800 feet high, and then carefully carried the apparatus to the top and repeated the measurement there while a control barometer was left at the bottom under the supervision of an assistant. Périer found the mercury column at the top of the mountain more than three inches shorter than at the bottom, whereas the length of the column in the control barometer had remained unchanged throughout the day.

2.3 The role of induction in scientific inquiry

We have considered some scientific investigations in which a problem was tackled by proposing tentative answers in the form of hypotheses that were then tested by deriving from them suitable test implications and checking these by observation or experiment.

But how are suitable hypotheses arrived at in the first place? It is sometimes held that they are inferred from antecedently collected data by means of a procedure called *inductive inference*, as distinguished from deductive inference, from which it differs in important respects.

In a deductively valid argument, the conclusion is related to the premises in such a way that if the premises are true then the conclusion cannot fail to be true as well. This requirement is satisfied, for example, by any argument of the following general form:

If p , then q .
It is not the case that q .

It is not the case that p .

Brief reflection shows that no matter what particular statements may stand at the places marked by the letters ' p ' and ' q ', the conclusion will certainly be true if the premises are. In fact, our schema represents the argument form called *modus tollens*, to which we referred earlier.

Another type of deductively valid inference is illustrated by this example:

Any sodium salt, when put into the flame of a Bunsen burner, turns the flame yellow.
This piece of rock salt is a sodium salt.

This piece of rock salt, when put into the flame of a Bunsen burner, will turn the flame yellow.

Arguments of the latter kind are often said to lead from the general (here, the premiss about all sodium salts) to the particular (a conclusion about the particular piece of rock salt). Inductive inferences, by contrast, are sometimes described as leading from premises about particular cases to a conclusion that has the character of a general law or principle. For example, from premises to the effect that each of the particular samples of various sodium salts that have so far been subjected to the Bunsen flame test did turn the flame yellow, inductive inference supposedly leads to the general conclusion that all sodium salts, when put into the flame of a Bunsen burner, turn the flame yellow. But in this case, the truth of the premises obviously does not guarantee the truth of the conclusion; for even if it is the case that all samples of sodium salts examined so far did turn the Bunsen flame yellow, it remains quite possible that new kinds of sodium salt might yet be found

that do not conform to this generalization. Indeed, even some kinds of sodium salt that have already been tested with positive result might conceivably fail to satisfy the generalization under special physical conditions (such as very strong magnetic fields or the like) in which they have not yet been examined. For this reason, the premises of an inductive inference are often said to imply the conclusion only with more or less high probability, whereas the premises of a deductive inference imply the conclusion with certainty.

The idea that in scientific inquiry, inductive inference from antecedently collected data leads to appropriate general principles is clearly embodied in the following account of how a scientist would ideally proceed:

If we try to imagine how a mind of superhuman power and reach, but normal so far as the logical processes of its thought are concerned, . . . would use the scientific method, the process would be as follows: First, all facts would be observed and recorded, *without selection or a priori guess as to their relative importance*. Secondly, the observed and recorded facts would be analyzed, compared, and classified, *without hypothesis or postulates other than those necessarily involved in the logic of thought*. Third, from this analysis of the facts generalizations would be inductively drawn as to the relations, classificatory or causal, between them. Fourth, further research would be deductive as well as inductive, employing inferences from previously established generalizations.⁵

This passage distinguishes four stages in an ideal scientific inquiry: (1) observation and recording of all facts, (2) analysis and classification of these facts, (3) inductive derivation of generalizations from them, and (4) further testing of the generalizations. The first two of these stages are specifically assumed not to make use of any guesses or hypotheses as to how the observed facts might be interconnected; this restriction seems to have been imposed in the belief that such preconceived ideas would introduce a bias and would jeopardize the scientific objectivity of the investigation.

But the view expressed in the quoted passage—I will call it *the narrow inductivist conception of scientific inquiry*—is untenable, for several reasons. A brief survey of these can serve to amplify and to supplement our earlier remarks on scientific procedure.

First, a scientific investigation as here envisaged could never get off the ground. Even its first phase could never be carried out, for a collection of *all* the facts would have to await the end of the world, so to speak; and even all the facts *up to now* cannot be collected, since there

⁵ A. B. Wolfe, "Functional Economics," in *The Trend of Economics*, ed. R. G. Tugwell (New York: Alfred A. Knopf, Inc., 1924), p. 450 (italics are quoted).

are an infinite number and variety of them. Are we to examine, for example, all the grains of sand in all the deserts and on all the beaches, and are we to record their shapes, their weights, their chemical composition, their distances from each other, their constantly changing temperature, and their equally changing distance from the center of the moon? Are we to record the floating thoughts that cross our minds in the tedious process? The shapes of the clouds overhead, the changing color of the sky? The construction and the trade name of our writing equipment? Our own life histories and those of our fellow investigators? All these, and untold other things, are, after all, among "all the facts up to now".

Perhaps, then, all that should be required in the first phase is that all the *relevant* facts be collected. But relevant to what? Though the author does not mention this, let us suppose that the inquiry is concerned with a specified *problem*. Should we not then begin by collecting all the facts—or better, all available data—relevant to that problem? This notion still makes no clear sense. Semmelweis sought to solve one specific problem, yet he collected quite different kinds of data at different stages of his inquiry. And rightly so; for what particular sorts of data it is reasonable to collect is not determined by the problem under study, but by a tentative answer to it that the investigator entertains in the form of a conjecture or hypothesis. Given the conjecture that mortality from childbed fever was increased by the terrifying appearance of the priest and his attendant with the death bell, it was relevant to collect data on the consequences of having the priest change his routine; but it would have been totally irrelevant to check what would happen if doctors and students disinfected their hands before examining their patients. With respect to Semmelweis' eventual contamination hypothesis, data of the latter kind were clearly relevant, and those of the former kind totally irrelevant.

Empirical "facts" or findings, therefore, can be qualified as logically relevant or irrelevant only in reference to a given hypothesis, but not in reference to a given problem.

Suppose now that a hypothesis *H* has been advanced as a tentative answer to a research problem: what kinds of data would be relevant to *H*? Our earlier examples suggest an answer: A finding is relevant to *H* if either its occurrence or its nonoccurrence can be inferred from *H*. Take Torricelli's hypothesis, for example. As we saw, Pascal inferred from it that the mercury column in a barometer should grow shorter if the barometer were carried up a mountain. Therefore, any finding to the effect that this did indeed happen in a particular case is relevant to the hypotheses; but so would be the finding that the length of the mercury column had remained unchanged or that it had decreased and then increased during the ascent, for such findings would refute Pascal's test

implication and would thus disconfirm Torricelli's hypothesis. Data of the former kind may be called positively, or favorably, relevant to the hypothesis; those of the latter kind negatively, or unfavorably, relevant.

In sum, the maxim that data should be gathered without guidance by antecedent hypotheses about the connections among the facts under study is self-defeating, and it is certainly not followed in scientific inquiry. On the contrary, tentative hypotheses are needed to give direction to a scientific investigation. Such hypotheses determine, among other things, what data should be collected at a given point in a scientific investigation.

It is of interest to note that social scientists trying to check a hypothesis by reference to the vast store of facts recorded by the U.S. Bureau of the Census, or by other data-gathering organizations, sometimes find to their disappointment that the values of some variable that plays a central role in the hypothesis have nowhere been systematically recorded. This remark is not, of course, intended as a criticism of data gathering: those engaged in the process no doubt try to select facts that might prove relevant to future hypotheses; the observation is simply meant to illustrate the impossibility of collecting "all the relevant data" without knowledge of the hypotheses to which the data are to have relevance.

The second stage envisaged in our quoted passage is open to similar criticism. A set of empirical "facts" can be analyzed and classified in many different ways, most of which will be unilluminating for the purposes of a given inquiry. Semmelweis could have classified the women in the maternity wards according to criteria such as age, place of residence, marital status, dietary habits, and so forth; but information on these would have provided no clue to a patient's prospects of becoming a victim of childbed fever. What Semmelweis sought were criteria that would be significantly connected with those prospects; and for this purpose, as he eventually found, it was illuminating to single out those women who were attended by medical personnel with contaminated hands; for it was with this characteristic, or with the corresponding class of patients, that high mortality from childbed fever was associated.

Thus, if a particular way of analyzing and classifying empirical findings is to lead to an explanation of the phenomena concerned, then it must be based on hypotheses about how those phenomena are connected; without such hypotheses, analysis and classification are blind.

Our critical reflections on the first two stages of inquiry as envisaged in the quoted passage also undercut the notion that hypotheses are introduced only in the third stage, by inductive inference from antecedently collected data. But some further remarks on the subject should be added here.

Induction is sometimes conceived as a method that leads, by means of mechanically applicable rules, from observed facts to corresponding general principles. In this case, the rules of inductive inference would provide effective canons of scientific discovery; induction would be a mechanical procedure analogous to the familiar routine for the multiplication of integers, which leads, in a finite number of predetermined and mechanically performable steps, to the corresponding product. Actually, however, no such general and mechanical induction procedure is available at present; otherwise, the much studied problem of the causation of cancer, for example, would hardly have remained unsolved to this day. Nor can the discovery of such a procedure ever be expected. For—to mention one reason—scientific hypotheses and theories are usually couched in terms that do not occur at all in the description of the empirical findings on which they rest, and which they serve to explain. For example, theories about the atomic and subatomic structure of matter contain terms such as 'atom', 'electron', 'proton', 'neutron', 'psi-function', etc.; yet they are based on laboratory findings about the spectra of various gases, tracks in cloud and bubble chambers, quantitative aspects of chemical reactions, and so forth—all of which can be described without the use of those "theoretical terms". Induction rules of the kind here envisaged would therefore have to provide a mechanical routine for constructing, on the basis of the given data, a hypothesis or theory stated in terms of some quite novel concepts, which are nowhere used in the description of the data themselves. Surely, no general mechanical rule of procedure can be expected to achieve this. Could there be a general rule, for example, which, when applied to the data available to Galileo concerning the limited effectiveness of suction pumps, would, by a mechanical routine, produce a hypothesis based on the concept of a sea of air?

To be sure, mechanical procedures for inductively "inferring" a hypothesis on the basis of given data may be specifiable for situations of special, and relatively simple, kinds. For example, if the length of a copper rod has been measured at several different temperatures, the resulting pairs of associated values for temperature and length may be represented by points in a plane coordinate system, and a curve may be drawn through them in accordance with some particular rule of curve fitting. The curve then graphically represents a general quantitative hypothesis that expresses the length of the rod as a specific function of its temperature. But note that this hypothesis contains no novel terms; it is expressible in terms of the concepts of temperature and length, which are used also in describing the data. Moreover, the choice of "associated" values of temperature and length as data already presupposes a guiding hypothesis; namely, that with each value of the tempera-

ture, exactly one value of the length of the copper rod is associated, so that its length is indeed a function of its temperature alone. The mechanical curve-fitting routine then serves only to select a particular function as the appropriate one. This point is important; for suppose that instead of a copper rod, we examine a body of nitrogen gas enclosed in a cylindrical container with a movable piston as a lid, and that we measure its volume at several different temperatures. If we were to use this procedure in an effort to obtain from our data a general hypothesis representing the volume of the gas as a function of its temperature, we would fail, because the volume of a gas is a function both of its temperature and of the pressure exerted upon it, so that at the same temperature, the given gas may assume different volumes.

Thus, even in these simple cases, the mechanical procedures for the construction of a hypothesis do only part of the job, for they presuppose an antecedent, less specific hypothesis (i.e., that a certain physical variable is a function of one single other variable), which is not obtainable by the same procedure.

There are, then, no generally applicable "rules of induction", by which hypotheses or theories can be mechanically derived or inferred from empirical data. The transition from data to theory requires creative imagination. Scientific hypotheses and theories are not derived from observed facts, but *invented* in order to account for them. They constitute guesses at the connections that might obtain between the phenomena under study, at uniformities and patterns that might underlie their occurrence. "Happy guesses" of this kind require great ingenuity, especially if they involve a radical departure from current modes of scientific thinking, as did, for example, the theory of relativity and quantum theory. The inventive effort required in scientific research will benefit from a thorough familiarity with current knowledge in the field. A complete novice will hardly make an important scientific discovery, for the ideas that may occur to him are likely to duplicate what has been tried before or to run afoul of well-established facts or theories of which he is not aware.

Nevertheless, the ways in which fruitful scientific guesses are arrived at are very different from any process of systematic inference. The

⁶ This characterization was given already by William Whewell in his work *The Philosophy of the Inductive Sciences*, 2nd ed. (London: John W. Parker, 1847); II, 41. Whewell also speaks of "invention" as "part of induction" (p. 46). In the same vein, K. Popper refers to scientific hypotheses and theories as "conjectures"; see, for example, the essay "Science: Conjectures and Refutations" in his book, *Conjectures and Refutations* (New York and London: Basic Books, 1962). Indeed, A. B. Wolfe, whose narrowly inductivist conception of ideal scientific procedure was quoted earlier, stresses that "the limited human mind" has to use "a greatly modified procedure", requiring scientific imagination and the selection of data on the basis of some "working hypothesis" (p. 450 of the essay cited in note 5).

chemist Kekulé, for example, tells us that he had long been trying unsuccessfully to devise a structural formula for the benzene molecule when, one evening in 1865, he found a solution to his problem while he was dozing in front of his fireplace. Gazing into the flames, he seemed to see atoms dancing in snakelike arrays. Suddenly, one of the snakes formed a ring by seizing hold of its own tail and then whirled mockingly before him. Kekulé awoke in a flash: he had hit upon the now famous and familiar idea of representing the molecular structure of benzene by a hexagonal ring. He spent the rest of the night working out the consequences of this hypothesis.⁷

This last remark contains an important reminder concerning the objectivity of science. In his endeavor to find a solution to his problem, the scientist may give free rein to his imagination, and the course of his creative thinking may be influenced even by scientifically questionable notions. Kepler's study of planetary motion, for example, was inspired by his interest in a mystical doctrine about numbers and a passion to demonstrate the music of the spheres. Yet, scientific objectivity is safeguarded by the principle that while hypotheses and theories may be freely invented and *proposed* in science, they can be *accepted* into the body of scientific knowledge only if they pass critical scrutiny, which includes in particular the checking of suitable test implications by careful observation or experiment.

Interestingly, imagination and free invention play a similarly important role in those disciplines whose results are validated exclusively by deductive reasoning; for example, in mathematics. For the rules of deductive inference do not afford mechanical rules of discovery, either. As illustrated by our statement of *modus tollens* above, those rules are usually expressed in the form of general schemata, any instance of which is a deductively valid argument. If premisses of the specified kind are given, such a schema does indeed specify a way of proceeding to a logical consequence. But for any set of premisses that may be given, the rules of deductive inference specify an infinity of validly deducible conclusions. Take, for example, one simple rule represented by the following schema:

$$\frac{p}{p \text{ or } q}$$

It tells us, in effect, that from the proposition that *p* is the case, it follows that *p* or *q* is the case, where *p* and *q* may be any propositions whatever. The word 'or' is here understood in the "nonexclusive" sense, so that '*p*

⁷ Cf. the quotations from Kekulé's own report in A. Findlay, *A Hundred Years of Chemistry*, 2nd ed. (London: Gerald Duckworth & Co., 1948), p. 37; and W.I.B. Beveridge, *The Art of Scientific Investigation*, 3rd ed. (London: William Heinemann, Ltd., 1957), p. 56.

or *q*' is tantamount to 'either *p* or *q* or both *p* and *q*'. Clearly, if the premiss of an argument of this type is true, then so must be the conclusion; hence, any argument of the specified form is valid. But this one rule alone entitles us to infer infinitely many different consequences from any one premiss. Thus, from 'the Moon has no atmosphere', it authorizes us to infer any statement of the form 'The Moon has no atmosphere, or *q*', where for '*q*' we may write any statement whatsoever, no matter whether it is true or false; for example, 'the Moon's atmosphere is very thin', 'the Moon is uninhabited', 'gold is denser than silver', 'silver is denser than gold', and so forth. (It is interesting and not difficult to prove that infinitely many different statements can be formed in English; each of these may be put in the place of the variable '*q*'.) Other rules of deductive inference add, of course, to the variety of statements derivable from one premiss or set of premisses. Hence, if we are given a set of statements as premisses, the rules of deduction give no direction to our inferential procedures. They do not single out one statement as "the" conclusion to be derived from our premisses, nor do they tell us how to obtain interesting or systematically important conclusions; they provide no mechanical routine, for example, for deriving significant mathematical theorems from given postulates. The discovery of important, fruitful mathematical theorems, like the discovery of important, fruitful theories in empirical science, requires inventive ingenuity; it calls for imaginative, insightful guessing. But again, the interests of scientific objectivity are safeguarded by the demand for an *objective validation* of such conjectures. In mathematics, this means *proof* by deductive derivation from axioms. And when a mathematical proposition has been proposed as a conjecture, its proof or disproof still requires inventiveness and ingenuity, often of a very high caliber; for the rules of deductive inference do not even provide a general mechanical procedure for constructing proofs or disproofs. Their systematic role is rather the modest one of serving as *criteria of soundness for arguments* offered as proofs: an argument will constitute a valid mathematical proof if it proceeds from the axioms to the proposed theorem by a chain of inferential steps each of which is valid according to one of the rules of deductive inference. And to check whether a given argument is a valid proof in this sense is indeed a purely mechanical task.

Scientific knowledge, as we have seen, is not arrived at by applying some inductive inference procedure to antecedently collected data, but rather by what is often called "the method of hypothesis", i.e. by inventing hypotheses as tentative answers to a problem under study, and then subjecting these to empirical test. It will be part of such test to see whether the hypothesis is borne out by whatever relevant findings may have been gathered before its formulation; an acceptable hypothesis

will have to fit the available relevant data. Another part of the test will consist in deriving new test implications from the hypothesis and checking these by suitable observations or experiments. As we noted earlier, even extensive testing with entirely favorable results does not establish a hypothesis conclusively, but provides only more or less strong support for it. Hence, while scientific inquiry is certainly not inductive in the narrow sense we have examined in some detail, it may be said to be *inductive in a wider sense*, inasmuch as it involves the acceptance of hypotheses on the basis of data that afford no deductively conclusive evidence for it, but lend it only more or less strong "inductive support", or confirmation. And any "rules of induction" will have to be conceived, in analogy to the rules of deduction, as canons of validation rather than of discovery. Far from generating a hypothesis that accounts for given empirical findings, such rules will presuppose that both the empirical data forming the "premises" of the "inductive argument" and a tentative hypothesis forming its "conclusion" are *given*. The rules of induction would then state criteria for the soundness of the argument. According to some theories of induction, the rules would determine the strength of the support that the data lend to the hypothesis, and they might express such support in terms of probabilities. In chapters 3 and 4 we will consider various factors that affect the inductive support and the acceptability of scientific hypotheses.

THE TEST OF A HYPOTHESIS: ITS LOGIC AND ITS FORCE

3

3.1 Experimental vs. nonexper- imental tests

Now we turn to a closer scrutiny of the reasoning on which scientific tests are based and of the conclusions that may be drawn from their outcomes. As before, we will use the word 'hypothesis' to refer to whatever statement is under test, no matter whether it purports to describe some particular fact or event or to express a general law or some other, more complex, proposition.

Let us begin with a simple remark, to which we will frequently have to refer in the subsequent discussion: the test implications of a hypothesis are normally of a conditional character; they tell us that *under specified test conditions*, an outcome of a certain kind will occur. Statements to this effect can be put into the following explicitly conditional form:

3a] If conditions of kind C are realized, then an event of kind E will occur.

For example, one of the hypotheses considered by Semmelweis yielded the test implication

If the patients in the First Division are delivered in lateral position, then their mortality from childbed fever will decrease.

And one of the test implications of his final hypothesis was

If the persons attending the women in the First Division wash their hands in a solution of chlorinated lime, then mortality from childbed fever will decrease.

Similarly, the test implications of Torricelli's hypothesis included conditional statements such as

If a Torricelli barometer is carried to increasing altitudes, then its mercury column will correspondingly decrease in length.

Such test implications are thus implications in a twofold sense: they are implications of the hypotheses from which they are derived, and they have the form of if then sentences, which in logic are called conditionals or material implications.

In each of the three examples just cited, the specified test conditions *C* are technologically realizable and can thus be brought about at will; and the realization of those conditions involves some control of a factor (position during delivery; absence or presence of infectious matter; pressure of the atmosphere overhead) that, according to the given hypothesis, affects the phenomenon under study (i.e., incidence of childbed fever in the first two cases; length of the mercury column in the third). Test implications of this kind provide a basis for an *experimental test*, which amounts to bringing about the conditions *C* and checking whether *E* occurs as implied by the hypothesis.

Many scientific hypotheses are expressed in quantitative terms. In the simplest case, they will then represent the value of one quantitative variable as a mathematical function of certain other variables. Thus, the classical gas law, $V = c \cdot T/P$, represents the volume of a body of gas as a function of its temperature and pressure (*c* is a constant factor). A statement of this kind yields indefinitely many quantitative test implications. In our example, these are of the following form: if the temperature of a body of gas is T_1 and its pressure is P_1 , then its volume is $c \cdot T_1/P_1$. And an experimental test then consists in varying the values of the "independent" variables and checking whether the "dependent" variable assumes the values implied by the hypothesis.

When experimental control is impossible, when the conditions *C* mentioned in the test implication cannot be brought about or varied by available technological means, then the hypothesis must be tested nonexperimentally, by seeking out, or waiting for, cases where the specified conditions are realized by nature, and then checking whether *E* does indeed occur.

It is sometimes said that in an experimental test of a quantitative hypothesis, only one of the quantities mentioned in the hypothesis is varied at a time, while all other conditions are kept constant. But this is impossible. In an experimental test of the gas law, for example, the pressure might be varied while the temperature is kept constant, or vice versa; but many other circumstances will change during the process—among them perhaps the relative humidity, the brightness of the illumi-

nation, and the strength of the magnetic field in the laboratory—and certainly the distance of the body of gas from the sun or moon. Not is there any reason to try to keep as many as possible of these factors constant if the experiment is to test the gas law as specified. For the law states that the volume of a given body of gas is fully determined by its temperature and its pressure. It implies therefore that other factors are "irrelevant to the volume" in the sense that changes in these factors do not affect the volume of the gas. To allow such other factors to vary is therefore to explore a wider range of cases in search of possible violations of the hypothesis under test.

Experimentation, however, is used in science not only as a method of test, but also as a method of discovery; and in this second context, as we will now see, the requirement that certain factors be kept constant makes good sense.

The use of experimentation as a method of test is illustrated by Torricelli's and Pécier's experiments. Here, a hypothesis has been antecedently advanced, and the experiment is performed to test it. In certain other cases, where no specific hypotheses have as yet been proposed, a scientist may start with a rough guess and may use experimentation as a guide to a more definite hypothesis. In studying how a metal wire is stretched by a weight suspended from it, he might conjecture that the quantitative increase in length will depend on the initial length of the wire, on its cross section, on the kind of metal it is made of, and on the weight of the body suspended from it. And he may then perform experiments to determine whether those factors do influence the increase in length (here, experimentation serves as a method of test), and if so, just how they affect the "dependent variable"—that is, just what the specific mathematical form of the dependence is (here, experimentation serves as a method of discovery). Knowing that the length of a wire varies also with its temperature, the experimenter will, first of all, keep the temperature constant, to eliminate the disturbing influence of this factor (though later on, he may systematically vary the temperature to ascertain whether the values of certain parameters in the functions connecting the length increase with the other factors are dependent on the temperature). In his experiments at constant temperature, he will vary the factors that he thinks are relevant, one at a time, keeping the others constant. On the basis of the results thus obtained, he will tentatively formulate generalizations that express the increase in length as a function of the unstretched length, of the weight, and so on; and from there, he may proceed to construct a more general formula representing the increase in length as a function of all the variables examined.

In cases of this kind, then, in which experimentation serves as a

heuristic device, as a guide to the discovery of hypotheses, the principle of keeping all but one of the "relevant factors" constant makes good sense. But, of course, the most that can be done is to keep constant all but one of those factors that are believed to be "relevant" in the sense of affecting the phenomenon under study: it is always possible that some other important factors may have been overlooked.

It is one of the striking characteristics, and one of the great methodological advantages, of natural science that many of its hypotheses admit of experimental test. But experimental testing of hypotheses cannot be said to be a distinctive characteristic of all and only the natural sciences. It does not mark a dividing line between natural and social science, for experimental testing procedures are used also in psychology and, if to a lesser extent, in sociology. Also, the scope of experimental testing increases steadily with the advances in the requisite technology. Moreover, not all hypotheses in the natural sciences permit of experimental test. Take, for example, the law formulated by Leavitt and Shapley for the periodic fluctuations in the brightness of a certain type of variable star, the so-called classical Cepheids. The law states that the longer the period P of such a star, i.e., the time interval between two successive states of maximal brightness, the greater is its intrinsic luminosity; in quantitative terms, $M = -(a + b \cdot \log P)$, where M is the magnitude, which by definition varies inversely with the brightness of the star. This law deductively implies any number of test sentences stating what the magnitude of a Cepheid will be if its period has this or that particular value, for example, 5.3 days or 17.5 days. But Cepheids with specific periods cannot be produced at will; hence, the law cannot be tested by experiment. Rather, the astronomer must search the skies for new Cepheids and must then try to ascertain whether their magnitude and period conform to the presumptive law.

3.2 The role of auxiliary hypotheses

We said earlier that test implications are "derived" or "inferred" from the hypothesis that is to be tested. This statement, however, gives only a rough indication of the relationship between a hypothesis and the sentences that serve as its test implications. In some cases, it is indeed possible deductively to infer from a hypothesis certain conditional statements that can serve as test sentences for it. Thus, as we saw, the Leavitt-Shapley law deductively implies sentences of the form: 'If star s is a Cepheid with a period of so many days, then its magnitude will be such and such'. But often the "derivation" of a test implication will be such and conclusive. Take, for example, Semmelweis' hypothesis that childbed fever is caused by contamination with infectious matter, and consider the test implication that if the persons attending the patients were to wash their hands in a solution

of chlorinated lime, then mortality from childbed fever would be reduced. This statement does not follow deductively from the hypothesis alone; its derivation presupposes the further premiss that unlike soap and water alone, a chlorinated lime solution will destroy the infectious matter. This premiss, which is tacitly taken for granted in the argument, plays the role of what we will call an *auxiliary assumption*, or *auxiliary hypothesis*, in deriving the test sentence from Semmelweis' hypothesis. Hence, we are not entitled to assert here that if the hypothesis H is true then so must be the test implication I , but only that if both H and the auxiliary hypothesis are true then so will be I . Reliance on auxiliary hypotheses, as we shall see, is the rule rather than the exception in the testing of scientific hypotheses; and it has an important consequence for the question whether an unfavorable test finding, i.e., one that shows I to be false, can be held to disprove the hypothesis under investigation.

If H alone implies I and if empirical findings show I to be false, then H must also be qualified as false: this follows by the *modus tollens* argument (2a). But when I is derived from H in conjunction with one or more auxiliary hypotheses A , then the schema (2a) must be replaced by the following one:

If both H and A are true, then so is I .

3b] But (as the evidence shows) I is not true.

H and A are not both true.

Thus if the test shows I to be false, we can infer only that either the hypothesis or one of the auxiliary assumptions included in A must be false; hence, the test provides no conclusive grounds for rejecting H . For example, if the antiseptic measure introduced by Semmelweis had not been followed by a decline in mortality, Semmelweis' hypothesis might still have been true: the negative test result might have been due to inefficacy of the chloride of lime solution as an antiseptic.

This kind of situation is not a mere abstract possibility. The astronomer Tycho Brahe, whose accurate observations provided the empirical basis for Kepler's laws of planetary motion, rejected the Copernican conception that the earth moves about the sun. He gave the following reason, among others: if the Copernican hypothesis were true, then the direction in which a fixed star would be seen by an observer on the earth at a fixed time of day should gradually change; for in the course of the annual travel of the earth about the sun, the star would be observed from a steadily changing vantage point—just as a child on a merry-go-round observes the face of an onlooker from a changing vantage point and therefore sees it in a constantly changing direction. More specifically, the direction from the observer to the star should vary periodically between two extremes, corresponding to opposite vantage points on the earth's

orbit about the sun. The angle subtended by these points is called the annual parallax of the star; the farther the star is from the earth, the smaller will be its parallax. Brahe, who made his observations before the telescope was introduced, searched with his most precise instruments for evidence of such "parallactic motions" of fixed stars—and found none. He therefore rejected the hypothesis of the earth's motion. But the test implication that the fixed stars show observable parallactic motions can be derived from Copernicus' hypothesis only with the help of the auxiliary assumption that the fixed stars are so close to the earth that their parallactic movements are large enough to be detected by means of Brahe's instruments. Brahe was aware of making this auxiliary assumption, and he believed that he had grounds for regarding it as true; hence he felt obliged to reject the Copernican conception. It has since been found that the fixed stars do show parallactic displacements, but that Brahe's auxiliary hypothesis was mistaken: even the nearest fixed stars are vastly more remote than he had assumed, and therefore parallactic measurements require powerful telescopes and very precise techniques. The first generally accepted measurement of a stellar parallax was made only in 1838.

The significance of auxiliary hypotheses in testing reaches still further. Suppose that a hypothesis H is tested by checking a test implication, 'If C then E ', which has been derived from H and a set A of auxiliary hypotheses. The test then ultimately comes to checking whether or not E does occur in a test situation in which, to the best of the investigator's knowledge, the conditions C are realized. If in fact this is not the case—if, for example, the test equipment is faulty or not sufficiently sensitive—then E may fail to occur even if both H and A are true. For this reason, the total set of auxiliary assumptions presupposed by the test may be said to include the supposition that the test arrangement satisfies the specified conditions C .

This point is particularly important when the hypothesis under scrutiny has stood up well in previous tests and is an essential part of a larger system of interconnected hypotheses that is also supported by diverse other evidence. In such a case, an effort will likely be made to account for the nonoccurrence of E by showing that some of the conditions C were not satisfied in the test.

As an example, consider the hypothesis that electric charges have an atomistic structure and are all of them integral multiples of the charge of the atom of electricity, the electron. This hypothesis received very impressive support from experiments conducted by R. A. Millikan in 1909 and later. In these experiments, the electric charges on individual, extremely small drops of some liquid such as oil or mercury were determined by measuring the velocities of the droplets while they were falling

in air under the influence of gravity or rising under the influence of a counteracting electric field. Millikan found all the charges either to be equal to, or to be small integral multiples of, a certain basic minimal charge, which he accordingly identified as the charge of the electron. On the basis of numerous careful measurements, he gave its value in electrostatic units as 4.774×10^{-10} . This hypothesis was soon challenged by the physicist Ehrenhaft in Vienna, who announced that he had repeated Millikan's experiment and had found charges that were considerably smaller than the electronic charge specified by Millikan. In his discussion of Ehrenhaft's results,¹ Millikan suggested several likely sources of error (i.e., violations of test requirements) that might account for Ehrenhaft's apparently adverse experimental findings: evaporation during observation, decreasing the weight of a droplet; formation of an oxide film on the mercury droplets used in some of Ehrenhaft's experiments; the disturbing influence of dust particles suspended in the air; the droplet drifting out of focus of the telescope used to observe it; deviation of very small droplets from the requisite spherical shape; inevitable errors in timing the movements of the small particles. In reference to two deviant particles observed and reported on by another investigator, who had experimented with oil drops, Millikan concludes: "The only possible interpretation then which could be put on these two particles . . . was that . . . they were not spheres of oil", but dust particles (pp. 170, 169). Millikan notes further that the results of more precise repetitions of his own experiment were all in essential accord with the result that he had announced earlier. Ehrenhaft continued for many years to defend and further expand his findings concerning subelectronic charges; but other physicists were not generally able to reproduce his results, and the atomistic conception of electric charge was maintained. Millikan's numerical value for the electronic charge, however, was later found to be slightly too small; interestingly, the deviation was traced to an error in one of Millikan's own auxiliary hypotheses: he had used too low a value for the viscosity of air in evaluating his oil drop data!

3.3 Crucial tests

The preceding remarks are of importance also for the idea of a crucial test, which can be briefly described as follows: suppose that H_1 and H_2 are two rival hypotheses concerning the same subject matter, which have so far stood up equally well in empirical tests, so that the available evidence does not favor one of them over the other. Then a decision between the two may be reached if some test can be specified for which H_1 and H_2 predict conflicting outcomes; i.e., if for a certain kind of test condition, C , the first hypothesis yields the test

¹ See Chap. VIII of R. A. Millikan, *The Electron* (Chicago: The University of Chicago Press, 1917). Reprinted, with an introduction by J.W.M. DuMond, 1963.

implication 'If C then E_1 ', and the second hypothesis yields 'If C then E_2 ', where E_1 and E_2 are mutually exclusive outcomes. Performance of the appropriate test will then presumably refute one of the hypotheses and support the other.

A classical example is the experiment performed by Foucault to decide between two competing conceptions of the nature of light. One of these, proposed by Huyghens and developed further by Fresnel and Young, held that light consists in transverse waves propagated in an elastic medium, the ether; the other was Newton's corpuscular conception, according to which light consists of extremely small particles traveling at high velocity. Either of these conceptions permitted the conclusion that light "rays" should conform to the laws of rectilinear propagation, reflection, and refraction. But the wave conception led to the further implication that light should travel faster in air than in water, whereas the corpuscular conception led to the opposite conclusion. In 1850, Foucault succeeded in performing an experiment in which the velocities of light in air and in water were directly compared. Images of two light-emitting points were produced by means of light rays that passed through water and through air, respectively, and were then reflected in a very rapidly revolving mirror. Depending on whether the velocity of light in air was greater or less than that in water, the image of the first light source would appear to the right or to the left of that of the second light source. The conflicting test implications checked by this experiment may therefore be briefly put as follows: 'if the Foucault experiment is performed, then the first image will appear to the right of the second image' and 'if the Foucault experiment is performed, then the first image will appear to the left of the second image'. The experiment showed the first of these implications to be true.

This outcome was widely regarded as a definitive refutation of the corpuscular conception of light and as a decisive vindication of the undulatory one. But this appraisal, though very natural, overrated the force of the test. For the statement that light travels faster in water than in air does not follow simply from the general conception of light rays as streams of particles; that assumption alone is much too indefinite to yield any specific quantitative consequences. Such implications as the laws of reflection and refraction and the statement about the velocities of light in air and in water can be derived only when the general corpuscular conception is supplemented by specific assumptions concerning the motion of the corpuscles and the influence exerted upon them by the surrounding medium. Newton did specify such assumptions; and in so doing, he set forth a definite *theory*² concerning the propagation of light. It is the total set of those basic theoretical principles that leads

² The form and function of theories will be further examined in Chap. 6.

to experimentally testable consequences such as the one checked by Foucault. Analogously, the wave conception was formulated as a *theory* based on a set of specific assumptions about the propagation of ether waves in different optical media; and again it is this set of theoretical principles that implied the laws of reflection and refraction and the statement that the velocity of light is greater in air than in water. Consequently—granting the truth of all other auxiliary hypotheses—the outcome of Foucault's experiment entitles us to infer only that not all the basic assumptions, or principles, of the corpuscular theory can be true—that at least one of them must be false. But it does not tell us which of them is to be rejected. Hence, it leaves open the possibility that the general conception of particle-like projectiles playing a role in the propagation of light might be retained in some modified form which would be characterized by a different set of basic laws.

And in fact, in 1905, Einstein did propound a modified version of the corpuscular conception in his theory of light quanta or photons, as they came to be called. The evidence he cited in support of his theory included an experiment performed by Lenard in 1903. Einstein characterized it as a "second crucial experiment" concerning the undulatory and corpuscular conceptions, and he noted that it "eliminated" the classical wave theory, in which by then the notion of elastic vibrations in the ether had been replaced by the idea, developed by Maxwell and Hertz, of transverse electromagnetic waves. Lenard's experiment, involving the photoelectric effect, could be regarded as testing two conflicting implications concerning the light energy that a radiating point P can transmit, during some fixed unit of time, to a small screen that is perpendicular to the light rays. On the classical wave theory, that energy will gradually and continuously decrease toward zero as the screen moves away from the point P ; on the photon theory, the energy must be at least that carried by a single photon—unless during the given time interval, no photon strikes the screen, in which case the energy received will be zero; hence, there will be no continuous decrease to zero. Lenard's experiment had borne out this latter alternative. Again, however, the wave conception was not definitely refuted; the outcome of the experiment showed only that *some* modification was needed in the system of basic assumptions of the wave theory. Einstein, in fact, endeavored to modify the classical theory as little as possible.³ In sum, then, an experiment of the kind here illustrated cannot strictly refute one of the two rival hypotheses.

But neither can it "prove" or definitively establish the other; for as was noted generally in section 2.2, scientific hypotheses or theories can-

³ This example is discussed at some length in Chap. 8 of P. Frank, *Philosophy of Science* (Englewood Cliffs, N.J.: Prentice-Hall, Spectrum Books, 1962).

not be conclusively proved by any set of available data, no matter how accurate and extensive. This is particularly obvious for hypotheses or theories that assert or imply general laws either for some process that is not directly observable—as in the case of the rival theories of light—or for some phenomenon more readily accessible to observation and measurement, such as free fall. Galileo's law, for example, refers to *all* instances of free fall in the past, present, and future; whereas all the relevant evidence available at any time can cover only that relatively small set of cases—all of them belonging to the past—in which careful measurements have been carried out. And even if Galileo's law were found to be strictly satisfied in all the observed cases, this would obviously not preclude the possibility that some unobserved cases in past or future may not conform to it. In sum, even the most careful and extensive test can neither disprove one of two hypotheses nor prove the other: thus strictly construed, a crucial experiment is impossible in science.⁴ But an experiment, such as Foucault's or Lenard's, may be crucial in a less strict, practical sense: it may reveal one of two conflicting theories as seriously inadequate and may lend strong support to its rival; and as a result, it may exert a decisive influence upon the direction of subsequent theorizing and experimentation.

3.4 Ad hoc hypotheses

If a particular way of testing a hypothesis *H* presupposes auxiliary assumptions A_1, A_2, \dots, A_n —i.e., if these are used as additional premisses in deriving from *H* the relevant test implication *I*—then, as we saw earlier, a negative test result, which shows *I* to be false, tells us only that *H* or one of the auxiliary hypotheses must be false and that a change must be made somewhere in this set of sentences if the test result is to be accommodated. A suitable adjustment might be made by modifying or completely abandoning *H* or by making changes in the system of auxiliary hypotheses. In principle, it would always be possible to retain *H* even in the face of seriously adverse test results—provided that we are willing to make sufficiently radical and perhaps burdensome revisions among our auxiliary hypotheses. But science is not interested in thus protecting its hypotheses or theories at all costs—and for good reasons. Consider an example. Before Torricelli introduced his conception of the pressure of the sea of air, the action of suction pumps was explained by the idea that nature abhors a vacuum and that, therefore, water rushes up the pump barrel to fill the vacuum created by the rising

⁴ This is the famous verdict of the French physicist and historian of science, Pierre Duhem. Cf. Part II, Chap. VI of his book, *The Aim and Structure of Physical Theory*, trans. P. P. Wiener (Princeton: Princeton University Press, 1954), originally published in 1905. In his Foreword to the English translation, Louis de Broglie includes some interesting observations on this idea.

piston. The same idea also served to explain several other phenomena. When Pascal wrote to Périer asking him to perform the Puy-de-Dôme experiment, he argued that the expected outcome would be a "decisive" refutation of that conception: "If it happens that the height of the quicksilver is less at the top than at the base of the mountain . . . it follows of necessity that the weight and pressure of the air is the sole cause of this suspension of the quicksilver, and not the abhorrence of a vacuum: for it is quite certain that there is much more air that presses on the foot of the mountain than there is on its summit, and one cannot well say that nature abhors a vacuum more at the foot of the mountain than at its summit."⁵ But the last remark actually indicates a way in which the conception of a *horror vacui* could be saved in the face of Périer's findings. Périer's results are decisive evidence against that conception only on the auxiliary assumption that the strength of the horror does not depend upon location. To reconcile Périer's apparently adverse evidence with the idea of a *horror vacui* it suffices to introduce instead the auxiliary hypothesis that nature's abhorrence of a vacuum decreases with increasing altitude. But while this assumption is not logically absurd or patently false, it is objectionable from the point of view of science. For it would be introduced *ad hoc*—i.e., for the sole purpose of saving a hypothesis seriously threatened by adverse evidence; it would not be called for by other findings and, roughly speaking, it leads to no additional test implications. The hypothesis of the pressure of air, on the other hand, does lead to further implications. Pascal mentions, for example, that if a partly inflated balloon were carried up a mountain, it would be more inflated at the mountaintop.

About the middle of the seventeenth century, a group of physicists, the plenists, held that a vacuum could not exist in nature; and in order to save this idea in the face of Torricelli's experiment, one of them offered the *ad hoc* hypothesis that the mercury in a barometer was being held in place by the "funiculus", an invisible thread by which it was suspended from the top of the inner surface of the glass tube. According to an initially very useful theory, developed early in the eighteenth century, the combustion of metals involves the escape of a substance called phlogiston. This conception was eventually abandoned in response to the experimental work of Lavoisier, who showed that the end product of the combustion process has greater weight than the original metal. But some tenacious adherents of the phlogiston theory tried to reconcile their conception with Lavoisier's finding by proposing the *ad hoc* hypoth-

⁵ From Pascal's letter of November 15, 1647 in I.H.B. and A.G.H. Spiers, trans., *The Physical Treatises of Pascal* (New York: Columbia University Press, 1937), p. 101.

esis that phlogiston had negative weight, so that its escape would increase the weight of the residue.

We should remember, however, that with the benefit of hindsight, it seems easy to dismiss certain scientific suggestions of the past as *ad hoc* hypotheses, whereas it may be quite difficult to pass judgment on a hypothesis proposed in a contemporary context. There is, in fact, no precise criterion for *ad hoc* hypotheses, though the questions suggested earlier provide some guidance: is the hypothesis proposed just for the purpose of saving some current conception against adverse evidence, or does it also account for other phenomena, does it yield further significant test implications? And one further relevant consideration is this: if more and more qualifying hypotheses have to be introduced to reconcile a certain basic conception with new evidence that becomes available, the resulting total system will eventually become so complex that it has to give way when a simple alternative conception is proposed.

3.5 Testability- in-principle and empirical import

As the preceding discussion shows, no statement or set of statements T can be significantly proposed as a scientific hypothesis or theory unless it is amenable to objective empirical test, at least "in principle". This is to say that it must be possible to derive from T , in the broad sense we have considered, certain test implications of the form 'if test conditions C are realized, then outcome E will occur'; but the test conditions need not be realized or technologically realizable at the time when T is propounded or contemplated. Take the hypothesis, for example, that the distance covered in t seconds by a body falling freely from rest near the surface of the moon is $s = 2.7 t^2$ feet. It yields deductively a set of test implications to the effect that the distances covered by such a body in 1, 2, 3, . . . seconds will be 2.7, 10.8, 24.3, . . . feet. Hence, the hypothesis is testable in principle, though it is as yet impossible to perform the test here specified.

But if a statement or set of statements is not testable at least in principle, in other words, if it has no test implications at all, then it cannot be significantly proposed or entertained as a scientific hypothesis or theory, for no conceivable empirical finding can then accord or conflict with it. In this case, it has no bearing whatever on empirical phenomena, or as we will also say, it lacks *empirical import*. Consider, for example, the view that the mutual gravitational attraction of physical bodies is a manifestation of certain "appetites or natural tendencies" closely related to love, inherent in those bodies, which make their "natural movements intelligible and possible".⁶ What test implications can be derived from this interpretation of gravitational phenomena? Considering some char-

⁶ This idea is set forth, for example, in J. F. O'Brien, "Gravity and Love as Unifying Principles," *The Thomist*, Vol. 21 (1958), 184-93.

acteristic aspects of love in the familiar sense, this view would seem to imply that gravitational affinity should be a selective phenomenon: not just any two physical bodies should attract each other. Nor should the strength of the affinity of one body to a second one always equal that of its converse, nor should it depend significantly on the masses of the bodies or on their distance. But since all of the consequences thus suggested are known to be false, the conception we are considering evidently is not meant to imply them. And indeed, that conception claims merely that the natural affinities underlying gravitational attraction are *related* to love. But, as will now be clear, this assertion is so elusive that it precludes the derivation of any test implications. No specific empirical findings of any kind are called for by this interpretation; no conceivable observational or experimental data can confirm or disconfirm it. In particular, therefore, it has no implications concerning gravitational phenomena; consequently, it cannot possibly explain those phenomena or render them "intelligible". To illustrate this further, let us suppose someone were to offer the alternative thesis that physical bodies gravitationally attract each other and tend to move toward each other from a natural tendency akin to hatred, from a natural inclination to collide with and destroy other physical objects. Would there be any conceivable way of adjudicating these conflicting views? Clearly not. Neither of them yields any testable implications; no empirical discrimination between them is possible. Not that the issue is "too deep" for scientific decision: the two verbally conflicting interpretations make no assertions at all. Hence, the question whether they are true or false makes no sense, and that is why scientific inquiry cannot possibly decide between them. They are *pseudo-hypotheses*: hypotheses in appearance only.

It should be borne in mind, however, that a scientific hypothesis normally yields test implications only when combined with suitable auxiliary-assumptions. Thus, Torricelli's conception of the pressure exerted by the sea of air yields definite test implications only on the assumption that air pressure is subject to laws analogous to those for water pressure; this assumption underlies, for example, the Puy-de-Dôme experiment. In judging whether a proposed hypothesis does have empirical import, we should ask ourselves, therefore, what auxiliary hypotheses are explicitly or tacitly presupposed in the given context, and whether in conjunction with the latter, the given hypothesis yields test implications (other than those that may be derivable from the auxiliary assumptions alone).

Moreover, a scientific idea will often be introduced in an initial form that offers only limited and tenuous possibilities for test; and on the basis of such initial tests it will gradually be given a more definite, precise, and diversely testable form.

For these reasons, and for certain others which would lead us too

far afield,⁷ it is not possible to draw a sharp dividing line between hypotheses and theories that are testable in principle and those that are not. But even though it is somewhat vague, the distinction here referred to is important and illuminating for appraising the significance and the potential explanatory efficacy of proposed hypotheses and theories.

⁷The issue is discussed further in another volume of this series: William Alston, *Philosophy of Language*, Chap. 4. A fuller, technical discussion will be found in the essay, "Empiricist Criteria of Cognitive Significance: Problems and Changes," in C. G. Hempel, *Aspects of Scientific Explanation* (New York: The Free Press, 1965).

CRITERIA OF CONFIRMATION AND ACCEPTABILITY

4

As we noted earlier, a favorable outcome of even very extensive and exacting tests cannot provide conclusive proof for a hypothesis, but only more or less strong evidential support, or confirmation. How strongly a hypothesis is supported by a given body of evidence depends on various characteristics of the evidence, which we will consider presently. In appraising what might be called the scientific acceptability or credibility of a hypothesis, one of the most important factors to consider is, of course, the extent and the character of the relevant evidence available and the resulting strength of the support it gives to the hypothesis. But several other factors have to be taken into account as well; these, too, will be surveyed in this chapter. We shall at first speak in a somewhat intuitive manner of more or less strong support, of small or large increments in confirmation, of factors that increase or decrease the credibility of a hypothesis, and the like. At the end of the chapter, we will briefly consider whether the concepts here referred to admit of a precise quantitative construal.

4.1 Quantity, variety, and precision of supporting evidence

In the absence of unfavorable evidence, the confirmation of a hypothesis will normally be regarded as increasing with the number of favorable test findings. For example, each new Cepheid variable whose period and luminosity are found to conform to the Leavitt-Shapley law will be considered as adding to the evidential support of the law. But broadly speaking, the increase in confirmation effected by one new favorable instance will generally become smaller as the number of previously established favorable instances grows. If thou-

sands of confirmatory cases are already available, the addition of one more favorable finding will raise the confirmation but little.

This remark must be qualified, however. If the earlier cases have all been obtained by tests of the same kind, but the new finding is the result of a different kind of test, the confirmation of the hypothesis may be significantly enhanced. For the confirmation of a hypothesis depends not only on the quantity of the favorable evidence available, but also on its variety: the greater the variety, the stronger the resulting support.

Suppose, for example, that the hypothesis under consideration is Snell's law, which states that a ray of light traveling obliquely from one optical medium into another is refracted at the separating surface in such a way that the ratio, $\sin \alpha / \sin \beta$, of the sines of the angles of incidence and of refraction is a constant for any pair of media. Compare now three sets of 100 tests each. In the first set, the media and the angle of incidence are kept constant: in each experiment, the ray passes from air into water at an angle of incidence of 30° ; the angle of refraction is measured. Suppose that in all cases, $\sin \alpha / \sin \beta$ does have the same value. In the second set, the media are kept constant, but the angle α is varied: light passes from air into water at varying angles; β is measured. Again, suppose that $\sin \alpha / \sin \beta$ has the same value in all cases. In the third set, both the media and the angle α are varied: 25 different pairs of media are examined: for each pair, four different angles α are used. Suppose that for each pair of media, the four associated values of the ratio $\sin \alpha / \sin \beta$ are equal, while the ratios associated with different pairs have different values.

Each test set then presents a class of favorable outcomes, since the ratios associated with any particular pair of media are found to be equal, as implied by Snell's law. But the third set, which offers the greatest variety of positive instances, will surely be regarded as supporting the law much more strongly than the second, which provides supporting instances of much more limited variety; and the first set, it will be agreed, lends even less strong support to the general law. In fact, it might seem that in the first set, the same experiment is performed over and over again, and that the positive outcome in all 100 cases can support the hypothesis no more strongly than do the first two tests in the set, which bear out the constancy of the ratio. But this idea is mistaken. What is repeated here 100 times is not literally the same experiment, for the successive performances differ in many respects, such as the distance of the apparatus from the moon, perhaps the temperature of the light source, the atmospheric pressure, and so on. What is "kept the same" is simply a certain set of conditions, including a fixed angle of incidence and one particular pair of media. And even if the first two or more measurements under these circumstances yield the same value for

$\sin \alpha / \sin \beta$, it is logically quite possible that subsequent tests under the specified circumstances should yield different values for the ratio. Thus even here, repeated tests with favorable outcome add to the confirmation of the hypothesis—though much less so than do tests that cover a wider variety of instances.

We might recall here that Semmelweis was able to point to a considerable variety of facts that lent evidential support to his final hypothesis. Scientific theories are often supported by empirical findings of amazing variety. Newton's theory of gravitation and of motion implies, for example, the laws for free fall, for the simple pendulum, for the motion of the moon about the earth and of the planets about the sun, for the orbits of comets and of man-made satellites, for the motion of double stars about each other, for tidal phenomena, and many more. And all the diverse experimental and observational findings that bear out those laws lend support to Newton's theory.

The reason why diversity of evidence is so important a factor in the confirmation of a hypothesis might be suggested by the following consideration, which refers to our example of various tests for Snell's law. The hypothesis under test—let us call it *S* for short—refers to *all* pairs of optical media and asserts that for any pair, the ratio $\sin \alpha / \sin \beta$ has the same value for *all* associated angles of incidence and of refraction. Now, the more widely a set of experiments ranges over the diverse possibilities here covered, the greater will be the chances of finding an unfavorable instance if *S* should be false. Thus, the first set of experiments may be said to test more specifically a hypothesis *S*₁ that expresses only a small part of Snell's law—namely, that $\sin \alpha / \sin \beta$ has the same value whenever the optical media are air and water and α is 30° . Hence, if *S*₁ should be true, but *S* false, the first kind of test will never disclose this. Similarly, the second set of experiments tests a hypothesis *S*₂, which asserts distinctly more than *S*₁, but still not nearly as much as *S*—namely, that $\sin \alpha / \sin \beta$ has the same value for all angles α and the associated angles β if the media involved are air and water. Hence, if *S*₂ should be true, but *S* false, a test set of the second kind would never disclose this. Thus, the third set of experiments might be said to test Snell's law more thoroughly than the other two; an entirely favorable outcome accordingly lends stronger support to it.

As an additional illustration of the power of diversified evidence, we might note that if the diversity of the evidence is still further increased by varying the temperature of the optical media or by using monochromatic light of different wave lengths, then Snell's law in the classical form cited above is in fact found to be false.

But have we not overstated the case for diversified evidence? After all, some ways of increasing variety would be regarded as pointless, as in-

capable of raising the confirmation of a hypothesis. This verdict would apply, for example, if in our first test set for Snell's law the variety were increased by having the experiment performed at different places, during different phases of the moon, or by experimenters with different eye color. But to try such variations would not be unreasonable if as yet we had no knowledge, or only extremely limited knowledge, of what factors are likely to affect optical phenomena. At the time of the Puy-de-Dôme experiment, for example, the experimenters had no very definite ideas of what factors other than altitude might affect the length of the mercury column in the barometer; and when Pascal's brother-in-law and his associates performed the Torricelli experiment on the mountaintop and found the mercury column over three inches shorter than it had been at the foot of the mountain, they decided to repeat the experiment then and there, changing the circumstances in various ways. As Périer says in his report: "I therefore tried the same thing five times more, with great accuracy, at different places on the top of the mountain, once under cover in the little chapel which is there, once exposed, once in a shelter, once in the wind, once in good weather, and once during the rain and the mists which came over us sometimes, having taken care to get rid of the air in the tube every time; and in all these trials there was found the same height of the quicksilver . . . ; this result fully satisfied us."¹

Thus, the qualification of certain ways of varying the evidence as important and of other ways as pointless is based on the background assumptions we entertain—perhaps as a result of previous research—concerning the probable influence of the factors to be varied upon the phenomenon with which the hypothesis is concerned.

And sometimes when such background assumptions are questioned and experimental variations are accordingly introduced which, on the generally accepted view, are pointless, a revolutionary discovery may be the outcome. This is illustrated by the recent overthrow of one of the basic background assumptions of physics, the principle of parity. According to this principle, the laws of nature are impartial between right and left; if a certain kind of physical process is possible (i.e., if its occurrence is not precluded by the laws of nature), then so is its mirror image (the process as seen in a reflecting mirror), where right and left are interchanged. In 1956, Yang and Lee, who were trying to account for some puzzling experimental findings concerning elementary particles, suggested that the principle of parity is violated in certain cases; and their bold hypothesis soon received clear experimental confirmation.

Sometimes, a test can be made more stringent, and its result the more weighty, by increasing the precision of the procedures of observa-

¹ W. F. Magie, ed., *A Source Book in Physics*, p. 74.

tion and measurement it involves. Thus, the hypothesis of the identity of inertial and gravitational mass—supported, for example, by the equality of the accelerations shown in free fall by bodies of different chemical constitution—has recently been re-examined with extremely precise methods; and the results, which have so far borne out the hypothesis, have greatly strengthened its confirmation.

4.2 Confirmation by "new" test implications

When a hypothesis is designed to explain certain observed phenomena, it will of course be so constructed that it implies their occurrence; hence, the fact to be explained will then constitute confirmatory evidence for it. But it is highly desirable for a scientific hypothesis to be confirmed also by "new" evidence—by facts that were not known or not taken into account when the hypothesis was formulated. Many hypotheses and theories in natural science have indeed received support from such "new" phenomena, with the result that their confirmation was considerably strengthened.

The point is well illustrated by an example that dates back to the last quarter of the nineteenth century, when physicists were searching for inherent regularities in the profusion of lines that had been found in the emission and absorption spectra of gases. In 1885, a Swiss school teacher, J. J. Balmer, proposed a formula that he thought expressed such a regularity for the wavelengths of a series of lines in the emission spectrum of hydrogen. On the basis of measurements that Angström had made of four lines in that spectrum, Balmer constructed the following general formula:

$$\lambda = b \frac{n^2}{n^2 - 2^2}$$

Here, b is a constant, whose value Balmer determined empirically as 3645.6 Å, and n is an integer greater than 2. For $n = 3, 4, 5,$ and $6,$ this formula yields values that agree very closely with those measured by Angström; but Balmer was confident that the other values, too, would represent wavelengths of lines yet to be measured—or even yet to be found—in the hydrogen spectrum. He was unaware that some further lines had already been noted and measured. By now, 35 consecutive lines in the so-called Balmer series for hydrogen have been ascertained, and all of these have wavelengths that agree well with the values predicted by Balmer's formula.²

It is hardly surprising that such striking confirmation by correctly predicted "new" facts greatly enhances the credence we will be prepared

² A full and lucid account, on which this brief survey is based, will be found in Chap. 33 of G. Holton and D.H.D. Roller, *Foundations of Modern Physical Science* (Reading, Mass.: Addison-Wesley Publishing Co., 1958).

to give to a hypothesis. A puzzling question arises in this context. Suppose for a moment that Balmer's formula had been constructed only after all the 35 lines now recorded in the series had been carefully measured. In this fictitious case, then, exactly the same experimental findings would be available that have in fact been obtained by measurements made in part before, and in much larger part after, the constructions of the formula. Should that formula be considered as less well confirmed in the fictitious case than in the actual one? It might seem reasonable to answer in the affirmative, on these grounds: for any given set of quantitative data, it is possible to construct a hypothesis that covers them, just as for any finite set of points, it is possible to draw a smooth curve that contains them all. Thus, there would be nothing very surprising about the construction of Balmer's formula in our fictitious case. What is remarkable, and does lend weight to a hypothesis, is its fitting "new" cases: and Balmer's hypothesis has this accomplishment to its credit in the actual case, but not in the fictitious one. But this argument could be met with the reply that even in the fictitious case, Balmer's formula is not just some otherwise arbitrary hypothesis that is rigged to fit the 35 measured wavelengths: it is, rather, a hypothesis of striking formal simplicity; and the very fact that it subsumes those 35 wavelengths under a mathematically simple formula should lend it much higher credibility than could be accorded to a very complex formula fitting the same data. To state the idea in geometrical terms: if a set of points representing the results of measurements can be connected by a simple curve, we have much greater confidence in having discovered an underlying general law than if the curve is complicated and shows no perceptible regularity. (This notion of simplicity will be further considered, later on in this chapter.) Besides, from a logical point of view, the strength of the support that a hypothesis receives from a given body of data should depend only on what the hypothesis asserts and what the data are: the question of whether the hypothesis or the data were presented first, being a purely historical matter, should not count as affecting the confirmation of the hypothesis. This latter conception is certainly implicit in recently developed statistical theories of testing and also in some contemporary logical analyses of confirmation and induction, to which brief reference will be made at the end of this chapter.

4.3 Theoretical support The support that may be claimed for a hypothesis need not all be of the inductive-evidential kind that we have considered so far: it need not consist entirely—or even partly—of data that bear out test implications derived from it. Support may also come "from above"; that is, from more inclusive hypotheses or theories that imply the given one and have independent evidential support. To illustrate: we con-

sidered earlier a hypothetical law for free fall on the moon, $s = 2.7 t^2$. Although none of its test implications have ever been checked by experiments on the moon, it has strong *theoretical support*, for it follows deductively from Newton's theory of gravitation and of motion (strongly supported by a highly diversified body of evidence) in conjunction with the information that the radius and the mass of the moon are .272 and .0123 of those of the earth and that the gravitational acceleration near the surface of the earth is 32.2 feet per second per second.

Similarly, the confirmation of a hypothesis that does have inductive evidential support will be further strengthened if, in addition, it acquires deductive support from above. This happened, for example, to Balmer's formula. Balmer had anticipated the possibility that the hydrogen spectrum might contain further series of lines, and that the wavelengths of all the lines might conform to a generalization of his formula; namely,

$$\lambda = b \frac{n^2}{n^2 - m^2}$$

Here, m is a positive integer, and n is any integer greater than m . For $m = 2$, this generalization yields Balmer's formula; whereas $m = 1, 3, 4, \dots$ determine new series of lines. And indeed, the existence of the series corresponding to $m = 1, 3, 4$, and 5 was later established by experimental exploration of the invisible infrared and ultraviolet parts of the hydrogen spectrum. Thus, there was strong evidential support for a more general hypothesis that implied Balmer's original formula as a special case, thus providing deductive support for it. And deductive support by a theory came in 1913, when the generalized formula—hence Balmer's original one, also—were shown by Bohr to be derivable from his theory of the hydrogen atom. This derivation greatly strengthened the support of Balmer's formula by fitting it into the context of quantum-theoretical conceptions developed by Planck, Einstein, and Bohr, which were supported by diverse evidence other than the spectroscopic measurements that lent inductive support to Balmer's formula.³

Correlatively, the credibility of a hypothesis will be adversely affected if it conflicts with hypotheses or theories that are accepted at the time as well-confirmed. In the *New York Medical Record* for 1877, a Dr. Caldwell of Iowa, reporting on an exhumation he claims to have witnessed, asserts that the hair and the beard of a man who had been buried clean-shaven, had burst the coffin and grown through the cracks.⁴ Although presented by a presumptive eyewitness, this statement will be

³ For details, see Holton and Roller, *Foundations of Modern Physical Science*, Chap. 34 (especially section 7).

⁴ B. Evans, *The Natural History of Nonsense* (New York: Alfred A. Knopf, 1946), p. 133.

rejected without much hesitation because it conflicts with well-established findings about the extent to which human hair continues to grow after death.

Our earlier discussion of Ehrenhaft's claim to have experimentally established the existence of subelectronic charges similarly illustrates the point that conflict with a broadly supported theory militates against a hypothesis.

The principle here referred to must be applied with discretion and restraint, however. Otherwise, it could be used to protect any accepted theory against overthrow: adverse findings could always be dismissed as conflicting with a well-established theory. Science does not, of course, follow this procedure; it is not interested in defending certain pet conceptions against all possible adverse evidence. It aims, rather, at a comprehensive body of sound empirical knowledge, represented by a well-confirmed system of empirical statements, and it is accordingly prepared to give up or to modify whatever hypotheses it may have previously accepted. But findings that are to dislodge a well-established theory have to be weighty; and adverse experimental results, in particular, have to be repeatable. Even when a strong and useful theory has been found to conflict with an experimentally reproducible "effect", it may still continue to be used in contexts where it is not expected to lead into difficulties. For example, when Einstein propounded the theory of light quanta to account for such phenomena as the photoelectric effect, he noted that in dealing with the reflection, refraction, and polarization of light, the electromagnetic wave theory would probably never be replaced; and it is indeed still used in this context. A large-scale theory that has been successful in many areas will normally be abandoned only when a more satisfactory alternative theory is available—and good theories are difficult to come by.⁵

4.4 Simplicity Another aspect that affects the acceptability of a hypothesis is its simplicity, compared with that of alternative hypotheses that would account for the same phenomena.

Consider a schematic illustration. Suppose that investigation of physical systems of a certain type (Cepheids, elastic metal springs, viscous liquids, or whatever) suggests to us that a certain quantitative characteristic, v , of such systems, might be a function of, and thus uniquely determined by, another such characteristic, u (in the way in

⁵ This point is suggestively presented and illustrated by reference to the phlogiston theory of combustion in Chap. 7 of J. B. Conant, *Science and Common Sense*. A provocative general conception of the rise and fall of scientific theories is developed in T. S. Kuhn's book *The Structure of Scientific Revolutions* (Chicago: The University of Chicago Press, 1962).

which the period of a pendulum is a function of its length). We therefore try to construct a hypothesis stating the exact mathematical form of the function. We have been able to check many instances in which u had one of the values 0, 1, 2, or 3; the associated values of v were regularly found to be 2, 3, 4, and 5, respectively. Suppose further that concerning these systems, we have no background knowledge that might bear on the likely form of the functional connection, and that the following three hypotheses have been proposed on the basis of our data:

$$H_1: v = u^4 - 6u^3 + 11u^2 - 5u + 2$$

$$H_2: v = u^3 - 4u^2 - u^3 + 16u^2 - 11u + 2$$

$$H_3: v = u + 2$$

Each of these fits the data: to each of the four u -values examined, it assigns exactly the v -value that has been found associated with it. In geometrical terms: if the three hypotheses are graphed in a plane coordinate system, then each of the resulting curves contains the four data-points (0,2), (1,3), (2,4), and (3,5).

Yet if, as has been assumed, we have no relevant background information that might indicate a different choice, we would no doubt favor H_3 over H_1 and H_2 on the ground that it is a simpler hypothesis than its rivals. This consideration suggests that if two hypotheses accord with the same data and do not differ in other respects relevant to their confirmation, the simpler one will count as more acceptable.

The relevance of the same basic idea to entire theories is often illustrated by reference to the Copernican heliocentric conception of the solar system, which was considerably simpler than the geocentric one it came to supersede, namely, Ptolemy's ingenious and accurate, but "grossly complicated system of main circles and sub-circles, with different radii, speeds, tilts, and different amounts and directions of eccentricity."⁶

Though, undeniably, simplicity is highly prized in science, it is not easy to state clear criteria of simplicity in the relevant sense and to justify the preference given to simpler hypotheses and theories.

Any criteria of simplicity would have to be objective, of course; they could not just refer to intuitive appeal or to the ease with which a hypothesis or theory can be understood or remembered, etc., for these factors vary from person to person. In the case of quantitative hypotheses like H_1 , H_2 , H_3 , one might think of judging simplicity by reference to the corresponding graphs. In rectangular coordinates, the graph of H_3 is

⁶ E. Rogers, *Physics for the Inquiring Mind* (Princeton: Princeton University Press, 1960), p. 240. Chapters 14 and 16 of this work offer a splendid description and appraisal of the two systems; they give more substance to the claim of greater simplicity for Copernicus' scheme, but show also that it was able to account for various facts, known at Copernicus' time, that the Ptolemaic system could not explain.

a straight line, whereas graphs of H_1 and H_2 are much more complicated curves through the four data-points. But this criterion seems arbitrary. For if the hypotheses are represented in polar coordinates, with u as the direction angle and v as the radius vector, then H_2 determines a spiral, whereas a function determining a "simple" straight line would be quite complicated.

When, as in our example, all the functions are expressed by polynomials, the order of the polynomial might serve as an index of complexity; thus H_2 would be more complex than H_1 , which in turn would be more complex than H_3 . But further criteria are needed when trigonometric and other functions are to be considered as well.

In the case of theories, the number of independent *basic assumptions* is sometimes suggested as an indicator of complexity. But assumptions can be combined and split up in many ways: there is no unambiguous way of counting them. For example, the statement that for any two points there is exactly one straight line containing them might be counted as expressing two assumptions rather than one; that there is at least one such line, and that there is at most one. And even if we could agree on the count, different basic assumptions might in turn differ in complexity and would then have to be weighed rather than counted. Similar remarks apply to the suggestion that the number of *basic concepts* used in a theory might serve as an index of its complexity. The question of criteria of simplicity has in recent years received a good deal of attention from logicians and philosophers, and some interesting results have been obtained, but no satisfactory general characterization of simplicity is available. As our examples suggest, however, there certainly are cases in which, even in the absence of explicit criteria, investigators would be in substantial agreement about which of two competing hypotheses or theories is the simpler.

Another intriguing problem concerning simplicity is that of justification: what reasons are there for following the *principle of simplicity*, as we might call it; that is, the maxim that the simpler of two otherwise equally confirmed rival hypotheses or theories is to be preferred, is to count as more acceptable?

Many great scientists have expressed the conviction that the basic laws of nature are simple. If this were known, there would indeed be a presumption that the simpler of two rival hypotheses is more likely to be true. But the assumption that the basic laws of nature are simple is of course at least as problematic as the soundness of the principle of simplicity and thus cannot provide a justification for it.

Some scientists and philosophers—among them Mach, Avenarius, Ostwald, and Pearson—have held that science seeks to give an economic or parsimonious description of the world, and that general hypotheses

purporting to express laws of nature are economic expedients for thought, serving to compress an indefinite number of particular cases (e.g., many cases of free fall) into one simple formula (e.g., Galileo's law); and from this point of view, it seems entirely reasonable to adopt the simplest among several competing hypotheses. This argument would be convincing if we had to choose between different *descriptions of one and the same set of facts*; but in adopting one among several competing hypotheses, such as H_1 , H_2 , H_3 above, we also adopt the *predictions* it implies concerning as yet untested cases; and in this respect, the hypotheses differ widely. Thus, for $u = 4$, H_1 , H_2 , and H_3 predict the v -values 150, 30, and 6, respectively. Now, H_3 may be mathematically simpler than its rivals; but what grounds are there for considering it more likely to be true, for basing our expectations concerning the as yet unexamined case $u = 4$ on H_3 rather than on one of the competing hypotheses, which fit the given data with the same precision?

One interesting answer has been suggested by Reichenbach.⁷ Briefly, he argues as follows: suppose that in our example v is indeed a function of u , $v = f(u)$. Let g be its graph in some system of coordinates; the choice is inessential. The true function f and its graph are, of course, unknown to the scientist who measures associated values of the two variables. Assuming, for the sake of the argument, that his measurements are exact, he will thus find a number of data-points that lie on the "true" curve g . Suppose now that in accordance with the principle of simplicity, the scientist draws the simplest, i.e., the intuitively smoothest, curve through those points. Then his graph, say g_1 , may deviate considerably from the true curve, though it does share at least the measured data-points with the latter. Put it as the scientist determines more and more data-points and plots further simplest graphs, g_2 , g_3 , g_4 , . . . , these will coincide more and more nearly with the true curve g , and the associated functions of f_2 , f_3 , f_4 , . . . will approximate more and more closely the true functional connection f . Thus, observance of the principle of simplicity cannot be *guaranteed* to yield the function f in one step or even in many; but if there is a functional connection between u and v , the procedure will gradually lead to a function that approximates the true one to any desired degree.

Reichenbach's argument, which has here been stated in a somewhat simplified form, is ingenious; but its force is limited. For no matter how far the construction of successive graphs and functions may have gone, the procedure affords no indication at all of how close an approximation to the true function has been attained—if indeed there is a true function at all. (As we noted earlier, for example, the volume of a body

⁷ H. Reichenbach, *Experience and Prediction* (Chicago: The University of Chicago Press, 1938), section 42.

of gas may seem to be, but is not in fact, a function of its temperature alone.) Moreover, the argument on grounds of convergence towards the true curve could be used also to justify certain other, intuitively complex and unreasonable methods of plotting graphs. For example, it is readily seen that if we were always to connect any two adjacent data-points by a semicircle whose diameter is the distance between the points, the resulting curves would eventually converge toward the true curve if there is one. Yet despite this "justification", this procedure would not be regarded as a sound way of forming quantitative hypotheses. Certain other nonsimple procedures, however—such as connecting adjacent data-points by hairpin loops whose length always exceeds a specified minimum value—are not justifiable in this fashion and can indeed be shown by Reichenbach's argument to be self-defeating. His idea is thus of distinct interest.

A very different view has been advanced by Popper. He construes the simpler of two hypotheses as the one that has greater empirical content, and he argues that the simpler hypothesis can therefore more readily be falsified (found out to be false), if indeed it should be false; and that this is of great importance to science, which seeks to expose its conjectures to the most thorough test and possible falsification. He summarizes his argument as follows: "Simple statements, if knowledge is our object, are to be prized more highly than less simple ones *because they tell us more; because their empirical content is greater; and because they are better testable.*"⁸ Popper makes his notion of degree of simplicity as degree of falsifiability more explicit by means of two different criteria. According to one of them, the hypothesis that the orbit of a given planet is a circle is simpler than the hypothesis that it is an ellipse, because the former could be falsified by the determination of four positions that are found not to lie on a circle (three positions can always be connected by a circle), whereas the falsification of the second hypothesis would require the determination of at least six positions of the planet. In this sense, the simpler hypothesis is here the more readily falsifiable one, and it is also stronger because it logically implies the less simple hypothesis. This criterion surely contributes to clarifying the kind of simplicity that is of concern to science.

But Popper alternatively calls one hypothesis more falsifiable, and hence simpler, than another if the first implies the second and thus has greater content in a strictly deductive sense. However, greater content is surely not always linked to greater simplicity. To be sure, sometimes a strong theory, such as Newton's theory of gravitation and motion, will

⁸ K. R. Popper, *The Logic of Scientific Discovery* (London: Hutchinson, 1959), p. 142 (italics are quoted). Chapters VI and VII of this book, which offer many illuminating observations on the role of simplicity in science, contain the presentation of the ideas here referred to.

be regarded as simpler than a vast array of unrelated laws of more limited scope that are implied by it. But the desirable kind of simplification thus achieved by a theory is not just a matter of increased content; for if two unrelated hypotheses (e.g., Hooke's and Snell's laws) are conjoined, the resulting conjunction tells us more, yet is not simpler, than either component. Also, of the three hypotheses H_1 , H_2 , H_3 considered above, none tells us more than any of the others; yet they do not count as equally simple. Nor do those three hypotheses differ in point of falsifiability. If false, any one of them can be shown to be false with the same ease—namely, by means of one counter-instance; for example, the data-pair (4, 10) would falsify them all.

Thus, while all the different ideas here briefly surveyed shed some light on the rationale of the principle of simplicity, the problems of finding a precise formulation and a unified justification for it are not as yet satisfactorily solved.⁹

4.5 The probability of hypotheses

Our survey of factors determining the credibility of scientific hypotheses shows that the credibility of a hypothesis H at a given time depends, strictly speaking, on the relevant parts of the total scientific knowledge at that time, including all the evidence relevant to the hypothesis and all the hypotheses and theories then accepted that have any bearing upon it; for as we have seen, it is by reference to these that the credibility of H has to be assessed. Strictly, therefore, we should speak of the *credibility of a hypothesis relative to a given body of knowledge*; the latter might be represented by a large set K of statements—all the statements accepted by science at the time.

The question naturally suggests itself whether it is possible to express this credibility in precise quantitative terms, by formulating a definition which, for any hypothesis H and any set K of statements, determines a number $c(H, K)$ expressing the degree of credibility that H possesses relative to K . And since we often speak of hypotheses as more or less probable, we might wonder further whether this quantitative concept could not be so defined as to satisfy all the basic principles of probability theory. In this case, the credibility of a hypothesis relative to any set K would be a real number no less than 0 and no greater than 1; a hypothesis that is true on purely logical grounds (such as "Tomorrow it will rain in Central Park or it won't") would always have the credibility 1; and finally, for any two logically incompatible statements H_1 and H_2 , the credibility of the hypothesis that one or the other of them is true

⁹ The reader who wishes to pursue these issues further will find the following discussions helpful: S. Barker, *Induction and Hypothesis* (Ithaca: Cornell University Press, 1957); "A Panel Discussion of Simplicity of Scientific Theories," *Philosophy of Science*, Vol. 28 (1961), 109-71; W. V. O. Quine, "On Simple Theories of a Complex World," *Synthese*, Vol. 15 (1963), 103-6.

would equal the sum of their credibilities: $c(H_1 \text{ or } H_2, K) = c(H_1, K) + c(H_2, K)$.

Various theories for such probabilities have indeed been proposed.¹⁰ They proceed from certain axioms like those just mentioned to a variety of more or less complex theorems that make it possible to determine certain probabilities *provided that others are already known*; but they offer no general definition of the probability of a hypothesis relative to given information!

And if the definition of the concept $c(H, K)$ is to take account of all the different factors we have surveyed, then the task is very difficult, to say the least; for as we saw, it is not even clear how such factors as the simplicity of a hypothesis, or the variety of its supporting evidence, are to be precisely characterized, let alone expressed in numerical terms.

However, certain illuminating and quite far-reaching results have recently been obtained by Carnap, who has studied the problem by reference to rigorously formalized model languages whose logical structure is considerably simpler than that required for the purpose of science. Carnap has developed a general method of defining what he calls the degree of confirmation for any hypothesis expressed in such a language with respect to any body of information expressed in the same language. The concept thus defined does satisfy all the principles of probability theory, and Carnap accordingly refers to it as the *logical or inductive probability* of the hypothesis relative to the given information.¹¹

¹⁰ One of them by the economist John Maynard Keynes, in his book, *A Treatise on Probability* (London: Macmillan & Company, Ltd., 1921).

¹¹ Carnap has given a brief and elementary account of the basic ideas in his article "Statistical and Inductive Probability," reprinted in E. H. Madden, ed., *The Structure of Scientific Thought* (Boston: Houghton Mifflin Company, 1960), pp. 269-79. A more recent, very illuminating statement is given in Carnap's article, "The Aim of Inductive Logic" in E. Nagel, P. Suppes, and A. Tarski, eds., *Logic, Methodology and Philosophy of Science. Proceedings of the 1960 International Congress* (Stanford: Stanford University Press, 1962), pp. 303-18.

LAWS AND THEIR ROLE IN SCIENTIFIC EXPLANATION

5

5.1 Two basic requirements for scientific explanations

To explain the phenomena of the physical world is one of the primary objectives of the natural sciences. Indeed, almost all of the scientific investigations that served as illustrations in the preceding chapters were aimed not at ascertaining some particular fact but at achieving some explanatory insight; they were concerned with questions such as how puerperal fever is contracted, why the water-lifting capacity of pumps has its characteristic limitation, why the transmission of light conforms to the laws of geometrical optics, and so forth. In this chapter and the next one, we will examine in some detail the character of scientific explanations and the kind of insight they afford.

That man has long and persistently been concerned to achieve some understanding of the enormously diverse, often perplexing, and sometimes threatening occurrences in the world around him is shown by the manifold myths and metaphors he has devised in an effort to account for the very existence of the world and of himself, for life and death, for the motions of the heavenly bodies, for the regular sequence of day and night, for the changing seasons, for thunder and lightning, sunshine and rain. Some of these explanatory ideas are based on anthropomorphic conceptions of the forces of nature, others invoke hidden powers or agents, still others refer to God's inscrutable plans or to fate.

Accounts of this kind undeniably may give the questioner a sense of having attained some understanding; they may resolve his perplexity and in this sense "answer" his question. But however satisfactory these answers may be psychologically, they are not adequate for the purposes of science, which, after all, is concerned to develop a conception of the world that has a clear, logical bearing on our experience and is thus

capable of objective test. Scientific explanations must, for this reason, meet two systematic requirements, which will be called the requirement of explanatory relevance and the requirement of testability.

The astronomer Francesco Sizi offered the following argument to show why, contrary to what his contemporary, Galileo, claimed to have seen through his telescope, there could be no satellites circling around Jupiter:

There are seven windows in the head, two nostrils, two ears, two eyes and a mouth; so in the heavens there are two favorable stars, two unpropitious, two luminaries, and Mercury alone undecided and indifferent. From which and many other similar phenomena of nature such as the seven metals, etc., which it were tedious to enumerate, we gather that the number of planets is necessarily seven. . . . Moreover, the satellites are invisible to the naked eye and therefore can have no influence on the earth and therefore would be useless and therefore do not exist.¹

The crucial defect of this argument is evident: the "facts" it adduces, even if accepted without question, are entirely irrelevant to the point at issue; they do not afford the slightest reason for the assumption that Jupiter has no satellites; the claim of relevance suggested by the barrage of words like 'therefore', 'it follows', and 'necessarily' is entirely spurious.

Consider by contrast the physical explanation of a rainbow. It shows that the phenomenon comes about as a result of the reflection and refraction of the white light of the sun in spherical droplets of water such as those that occur in a cloud. By reference to the relevant optical laws, this account shows that the appearance of a rainbow is to be expected whenever a spray or mist of water droplets is illuminated by a strong white light behind the observer. Thus, even if we happened never to have seen a rainbow, the explanatory information provided by the physical account would constitute good grounds for expecting or believing that a rainbow will appear under the specified circumstances. We will refer to this characteristic by saying that the physical explanation meets the requirement of explanatory relevance: the explanatory information adduced affords good grounds for believing that the phenomenon to be explained did, or does, indeed occur. This condition must be met if we are to be entitled to say: "That explains it—the phenomenon in question was indeed to be expected under the circumstances!"

The requirement represents a necessary condition for an adequate explanation, but not a sufficient one. For example, a large body of data

¹ From Holton and Roller, *Foundations of Modern Physical Science*, p. 160.

showing a red-shift in the spectra of distant galaxies provides strong grounds for believing that those galaxies recede from our local one at enormous speeds, yet it does not explain why.

To introduce the second basic requirement for scientific explanations, let us consider once more the conception of gravitational attraction as manifesting a natural tendency akin to love. As we noted earlier, this conception has no test implications whatever. Hence, no empirical finding could possibly bear it out or disconfirm it. Being thus devoid of empirical content, the conception surely affords no grounds for expecting the characteristic phenomena of gravitational attraction: it lacks objective explanatory power. Similar comments apply to explanations in terms of an inscrutable fate: to invoke such an idea is not to achieve an especially profound insight, but to give up the attempt at explanation altogether. By contrast, the statements on which the physical explanation of a rainbow is based do have various test implications; these concern, for example, the conditions under which a rainbow will be seen in the sky, and the order of the colors in it; the appearance of rainbow phenomena in the spray of a wave breaking on the rocks and in the mist of a lawn sprinkler; and so forth. These examples illustrate a second condition for scientific explanations, which we will call the requirement of testability: the statements constituting a scientific explanation must be capable of empirical test.

It has already been suggested that since the conception of gravitation in terms of an underlying universal affinity has no test implications, it can have no explanatory power: it cannot provide grounds for expecting that universal gravitation will occur, nor that gravitational attraction will show such and such characteristic features; for if it did imply such consequences either deductively or even in a weaker, inductive-probabilistic sense, then it would be testable by reference to those consequences. As this example shows, the two requirements just considered are interrelated: a proposed explanation that meets the requirement of relevance also meets the requirement of testability. (The converse clearly does not hold.)

Now let us see what forms scientific explanations take, and how they meet the two basic requirements.

5.2 Deductive-nomological explanation

Consider once more Pèrier's finding in the Puy-de-Dôme experiment, that the length of the mercury column in a Torricelli barometer decreased with increasing altitude. Torricelli's and Pascal's ideas on atmospheric pressure provided an explanation for this phenomenon; somewhat pedantically, it can be spelled out as follows:

- d] At any location, the pressure that the mercury column in the closed branch of the Torricelli apparatus exerts upon the mercury below equals the pressure exerted on the surface of the mercury in the open vessel by the column of air above it.
- e] The pressures exerted by the columns of mercury and of air are proportional to their weights; and the shorter the columns, the smaller their weights.
- f] As Périer carried the apparatus to the top of the mountain, the column of air above the open vessel became steadily shorter.
- g] (Therefore,) the mercury column in the closed vessel grew steadily shorter during the ascent.

Thus formulated, the explanation is an argument to the effect that the phenomenon to be explained, as described by the sentence (d), is just what is to be expected in view of the explanatory facts cited in (a), (b), and (c); and that, indeed, (d) follows deductively from the explanatory statements. The latter are of two kinds; (a) and (b) have the character of general laws expressing uniform empirical connections; whereas (c) describes certain particular facts. Thus, the shortening of the mercury column is here explained by showing that it occurred in accordance with certain laws of nature, as a result of certain particular circumstances. The explanation fits the phenomenon to be explained into a pattern of uniformities and shows that its occurrence was to be expected, given the specified laws and the pertinent particular circumstances.

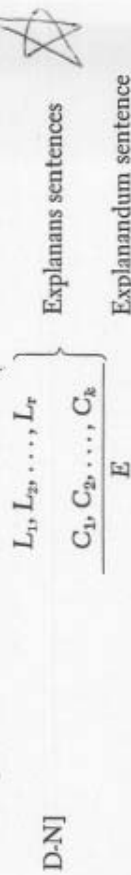
The phenomenon to be accounted for by an explanation will henceforth also be referred to as the *explanandum phenomenon*; the sentence describing it, as the *explanandum sentence*. When the context shows which is meant, either of them will simply be called the *explanandum*. The sentences specifying the explanatory information—(a), (b), (c) in our example—will be called the *explanans sentences*; jointly they will be said to form the *explanans*.

As a second example, consider the explanation of a characteristic of image formation by reflection in a spherical mirror; namely, that generally $1/u + 1/v = 2/r$, where u and v are the distances of object-point and image-point from the mirror, and r is the mirror's radius of curvature. In geometrical optics, this uniformity is explained with the help of the basic law of reflection in a plane mirror, by treating the reflection of a beam of light at any one point of a spherical mirror as a case of reflection in a plane tangential to the spherical surface. The resulting explanation can be formulated as a deductive argument whose conclusion is the *explanandum sentence*, and whose premisses include the basic laws of

reflection and of rectilinear propagation, as well as the statement that the surface of the mirror forms a segment of a sphere.²

A similar argument, whose premisses again include the law for reflection in a plane mirror, offers an explanation of why the light of a small light source placed at the focus of a paraboloidal mirror is reflected in a beam parallel to the axis of the paraboloid (a principle technologically applied in the construction of automobile headlights, searchlights, and other devices).

The explanations just considered may be conceived, then, as deductive arguments whose conclusion is the *explanandum sentence*, E , and whose premiss-set, the *explanans*, consists of general laws, L_1, L_2, \dots, L_r , and of other statements, C_1, C_2, \dots, C_k , which make assertions about particular facts. The form of such arguments, which thus constitute one type of scientific explanation, can be represented by the following schema:



Explanatory accounts of this kind will be called *explanations* by deductive subsumption under general laws, or *deductive-nomological explanations*. (The root of the term 'nomological' is the Greek word 'nomos', for law.) The laws invoked in a scientific explanation will also be called *covering laws* for the explanandum phenomenon, and the explanatory argument will be said to subsume the explanandum under those laws.

The explanandum phenomenon in a deductive-nomological explanation may be an event occurring at a particular place and time, such as the outcome of Périer's experiment. Or it may be some regularity found in nature, such as certain characteristics generally displayed by rainbows; or a uniformity expressed by an empirical law such as Galileo's or Kepler's laws. Deductive explanations of such uniformities will then invoke laws of broader scope, such as the laws of reflection and refraction, or Newton's laws of motion and of gravitation. As this use of Newton's laws illustrates, empirical laws are often explained by means of theoretical principles that refer to structures and processes underlying the uniformities in question. We will return to such explanations in the next chapter.

² The derivation of the laws of reflection for the curved surfaces referred to in this example and in the next one is simply and lucidly set forth in Chap. 17 of Morris Kline, *Mathematics and the Physical World* (New York: Thomas Y. Crowell Company, 1959).

Deductive-nomological explanations satisfy the requirement of explanatory relevance in the strongest possible sense: the explanatory information they provide implies the explanandum sentence deductively and thus offers logically conclusive grounds why the explanandum phenomenon is to be expected. (We will soon encounter other scientific explanations, which fulfill the requirement only in a weaker, inductive, sense.) And the testability requirement is met as well, since the explanans implies among other things that under the specified conditions, the explanandum phenomenon occurs.

Some scientific explanations conform to the pattern (D-N) quite closely. This is so, particularly, when certain quantitative features of a phenomenon are explained by mathematical derivation from covering general laws, as in the case of reflection in spherical and paraboloidal mirrors. Or take the celebrated explanation, propounded by Leverrier (and independently by Adams), of peculiar irregularities in the motion of the planet Uranus, which on the current Newtonian theory could not be accounted for by the gravitational attraction of the other planets then known. Leverrier conjectured that they resulted from the gravitational pull of an as yet undetected outer planet, and he computed the position, mass, and other characteristics which that planet would have to possess to account in quantitative detail for the observed irregularities. His explanation was strikingly confirmed by the discovery, at the predicted location, of a new planet, Neptune, which had the quantitative characteristics attributed to it by Leverrier. Here again, the explanation has the character of a deductive argument whose premisses include general laws—specifically, Newton's laws of gravitation and of motion—as well as statements specifying various quantitative particulars about the disturbing planet.

Not infrequently, however, deductive-nomological explanations are stated in an elliptical form: they omit mention of certain assumptions that are presupposed by the explanation but are simply taken for granted in the given context. Such explanations are sometimes expressed in the form 'E because C', where E is the event to be explained and C is some antecedent or concomitant event or state of affairs. Take, for example, the statement: 'The slush on the sidewalk remained liquid during the frost because it had been sprinkled with salt'. This explanation does not explicitly mention any laws, but it tacitly presupposes at least one: that the freezing point of water is lowered whenever salt is dissolved in it. Indeed, it is precisely by virtue of this law that the sprinkling of salt acquires the explanatory, and specifically causative, role that the elliptical because-statement ascribes to it. That statement, incidentally, is elliptical also in other respects; for example, it tacitly takes for granted, and leaves unmentioned, certain assumptions about the prevailing physical

conditions, such as the temperature's not dropping to a very low point. And if nomic and other assumptions thus omitted are added to the statement that salt had been sprinkled on the slush, we obtain the premisses for a deductive-nomological explanation of the fact that the slush remained liquid.

Similar comments apply to Semmelweis's explanation that childbed fever was caused by decomposed animal matter introduced into the bloodstream through open wound surfaces. Thus formulated, the explanation makes no mention of general laws; but it presupposes that such contamination of the bloodstream generally leads to blood poisoning attended by the characteristic symptoms of childbed fever, for this is implied by the assertion that the contamination causes puerperal fever. The generalization was no doubt taken for granted by Semmelweis, to whom the cause of Kolletschka's fatal illness presented no etiological problem: given that infectious matter was introduced into the bloodstream, blood poisoning would result. (Kolletschka was by no means the first one to die of blood poisoning resulting from a cut with an infected scalpel. And by a tragic irony, Semmelweis himself was to suffer the same fate.) But once the tacit premiss is made explicit, the explanation is seen to involve reference to general laws.

As the preceding examples illustrate, corresponding general laws are always presupposed by an explanatory statement to the effect that a particular event of a certain kind G (e.g., expansion of a gas under constant pressure; flow of a current in a wire loop) was caused by an event of another kind, F (e.g., heating of the gas; motion of the loop across a magnetic field). To see this, we need not enter into the complex ramifications of the notion of cause; it suffices to note that the general maxim "Same cause, same effect", when applied to such explanatory statements, yields the implied claim that whenever an event of kind F occurs, it is accompanied by an event of kind G.

To say that an explanation rests on general laws is not to say that its discovery required the discovery of the laws. The crucial new insight achieved by an explanation will sometimes lie in the discovery of some particular fact (e.g., the presence of an undetected outer planet; infectious matter adhering to the hands of examining physicians) which, by virtue of antecedently accepted general laws, accounts for the explanandum phenomenon. In other cases, such as that of the lines in the hydrogen spectrum, the explanatory achievement does lie in the discovery of a covering law (Balmer's) and eventually of an explanatory theory (such as Bohr's); in yet other cases, the major accomplishment of an explanation may lie in showing that, and exactly how, the explanandum phenomenon can be accounted for by reference to laws and data about particular facts that are already available: this is illustrated by the ex-

planatory derivation of the reflection laws for spherical and paraboloidal mirrors from the basic law of geometrical optics in conjunction with statements about the geometrical characteristics of the mirrors.

An explanatory problem does not by itself determine what kind of discovery is required for its solution. Thus, Leverrier discovered deviations from the theoretically expected course also in the motion of the planet Mercury; and as in the case of Uranus, he tried to explain these as resulting from the gravitational pull of an as yet undetected planet, Vulcan, which would have to be a very dense and very small object between the sun and Mercury. But no such planet was found, and a satisfactory explanation was provided only much later by the general theory of relativity, which accounted for the irregularities not by reference to some disturbing particular factor, but by means of a new system of laws.

5.3 Universal laws and accidental generalizations

As we have seen, laws play an essential role in deductive-nomological explanations. They provide the link by reason of which particular circumstances (described by C_1, C_2, \dots, C_k) can serve to explain the occurrence of a given event. And when the explanandum is not a particular event, but a uniformity such as those represented by characteristics mentioned earlier of spherical and paraboloidal mirrors, the explanatory laws exhibit a system of more comprehensive uniformities, of which the given one is but a special case.

The laws required for deductive-nomological explanations share a basic characteristic: they are, as we shall say, statements of universal form. Broadly speaking, a statement of this kind asserts a uniform connection between different empirical phenomena or between different aspects of an empirical phenomenon. It is a statement to the effect that whenever and wherever conditions of a specified kind F occur, then so will, always and without exception, certain conditions of another kind, G . (Not all scientific laws are of this type. In the sections that follow, we will encounter laws of probabilistic form, and explanations based on them.)

Here are some examples of statements of universal form: whenever the temperature of a gas increases while its pressure remains constant, its volume increases; whenever a solid is dissolved in a liquid, the boiling point of the liquid is raised; whenever a ray of light is reflected at a plane surface, the angle of reflection equals the angle of incidence; whenever a magnetic iron rod is broken in two, the pieces are magnets again; whenever a body falls freely from rest in a vacuum near the surface of the earth, the distance it covers in t seconds is $16t^2$ feet. Most of the laws of the natural sciences are quantitative: they assert specific mathematical connections between different quantitative characteristics of physical systems (e.g., between volume, temperature, and pressure of a gas) or of

processes (e.g., between time and distance in free fall in Galileo's law; between the period of revolution of a planet and its mean distance from the sun, in Kepler's third law; between the angles of incidence and refraction in Snell's law).

Strictly speaking, a statement asserting some uniform connection will be considered a law only if there are reasons to assume it is true: we would not normally speak of false laws of nature. But if this requirement were rigidly observed, then the statements commonly referred to as Galileo's and Kepler's laws would not qualify as laws; for according to current physical knowledge, they hold only approximately; and as we shall see later, physical theory explains why this is so. Analogous remarks apply to the laws of geometrical optics. For example, even in a homogeneous medium, light does not move strictly in straight lines: it can bend around corners. We shall therefore use the word "law" somewhat liberally, applying the term also to certain statements of the kind here referred to, which, on theoretical grounds, are known to hold only approximately and with certain qualifications. We shall return to this point when, in the next chapter, we consider the explanation of laws by theories.

We saw that the laws invoked in deductive-nomological explanations have the basic form: 'In all cases when conditions of kind F are realized, conditions of kind G are realized as well'. But, interestingly, not all statements of this universal form, even if true, can qualify as laws of nature. For example, the sentence 'All rocks in this box contain iron' is of universal form (F is the condition of being a rock in the box, G that of containing iron); yet even if true, it would not be regarded as a law, but as an assertion of something that "happens to be the case", as an "accidental generalization". Or consider the statement: 'All bodies consisting of pure gold have a mass of less than 100,000 kilograms'. No doubt all bodies of gold ever examined by man conform to it; thus, there is considerable confirmatory evidence for it and no disconfirming instances are known. Indeed, it is quite possible that never in the history of the universe has there been or will there be a body of pure gold with a mass of 100,000 kilograms or more. In this case, the proposed generalization would not only be well confirmed, but true. And yet, we would presumably regard its truth as accidental, on the ground that nothing in the basic laws of nature as conceived in contemporary science precludes the possibility of there being—or even the possibility of our producing—a solid gold object with a mass exceeding 100,000 kilograms.

Thus, a scientific law cannot be adequately defined as a true statement of universal form: this characterization expresses a necessary, but not a sufficient, condition for laws of the kind here under discussion. What distinguishes genuine laws from accidental generalizations?

This intriguing problem has been intensively discussed in recent years. Let us look briefly at some of the principal ideas that have emerged from the debate, which is still continuing.

One telling and suggestive difference, noted by Nelson Goodman,³ is this: a law can, whereas an accidental generalization cannot, serve to support *counterfactual conditionals*, i.e., statements of the form 'If A were (had been) the case, then B would be (would have been) the case', where in fact A is not (has not been) the case. Thus, the assertion 'If this paraffin candle had been put into a kettle of boiling water, it would have melted' could be supported by adducing the law that paraffin is liquid above 60 degrees centigrade (and the fact that the boiling point of water is 100 degrees centigrade). But the statement 'All rocks in this box contain iron' could not be used similarly to support the counterfactual statement 'If this pebble had been put into the box, it would contain iron'. Similarly, a law, in contrast to an accidentally true generalization, can support *subjunctive conditionals*, i.e., sentences of the type 'If A should come to pass, then so would B', where it is left open whether or not A will in fact come to pass. The statement 'If this paraffin candle should be put into boiling water then it would melt' is an example.

Closely related to this difference is another one, which is of special interest to us: a law can, whereas an accidental generalization cannot, serve as a basis for an explanation. Thus, the melting of a particular paraffin candle that was put into boiling water can be explained, in conformity with the schema (D-N), by reference to the particular facts just mentioned and to the law that paraffin melts when its temperature is raised above 60 degrees centigrade. But the fact that a particular rock in the box contains iron cannot be analogously explained by reference to the general statement that all rocks in the box contain iron.

It might seem plausible to say, by way of a further distinction, that the latter statement simply serves as a conveniently brief formulation of a finite conjunction of this kind: 'Rock r_1 contains iron, and rock r_2 contains iron, . . . , and rock r_{103} contains iron'; whereas the generalization about paraffin refers to a potentially infinite set of particular cases and therefore cannot be paraphrased by a finite conjunction of statements describing individual instances. This distinction is suggestive, but it is overstated. For to begin with, the generalization 'All rocks in this box contain iron' does not in fact tell us how many rocks there are in the box, nor does it name any particular rocks r_1, r_2 , etc. Hence, the general

³ In his essay, "The Problem of Counterfactual Conditionals," reprinted as the first chapter of his book, *Fact, Fiction, and Forecast*, 2nd ed. (Indianapolis: The Bobbs-Merrill Co., Inc., 1965). This work raises fascinating basic problems concerning laws, counterfactual statements, and inductive reasoning, and examines them from an advanced analytic point of view.

sentence is not logically equivalent to a finite conjunction of the kind just mentioned. To formulate a suitable conjunction, we need additional information, which might be obtained by counting and labeling the rocks in the box. Besides, our generalization 'All bodies of pure gold have a mass of less than 100,000 kilograms' would not count as a law even if there were infinitely many bodies of gold in the world. Thus, the criterion we have under consideration fails on several grounds.

Finally, let us note that a statement of universal form may qualify as a law even if it actually has no instances whatever. As an example, consider the sentence: 'On any celestial body that has the same radius as the earth but twice its mass, free fall from rest conforms to the formula $s = 32t^2$ '. There might well be no celestial object in the entire universe that has the specified size and mass, and yet the statement has the character of a law. For it (or rather, a close approximation of it, as in the case of Galileo's law) follows from the Newtonian theory of gravitation and of motion in conjunction with the statement that the acceleration of free fall on the earth is 32 feet per second per second; thus, it has strong theoretical support, just like our earlier law for free fall on the moon.

A law, we noted, can support subjunctive and counterfactual conditional statements about potential instances, i.e., about particular cases that might occur, or that might have occurred but did not. In similar fashion, Newton's theory supports our general statement in a subjunctive version that suggests its lawlike status, namely: 'On any celestial body that there may be which has the same size as the earth but twice its mass, free fall would conform to the formula $s = 32t^2$ '. By contrast, the generalization about the rocks cannot be paraphrased as asserting that any rock that might be in this box would contain iron, nor of course would this latter claim have any theoretical support.

Similarly, we would not use our generalization about the mass of gold bodies—let us call it *H*—to support statements such as this: 'Two bodies of pure gold whose individual masses add up to more than 100,000 kilograms cannot be fused to form one body; or if fusion should be possible, then the mass of the resulting body will be less than 100,000 kg', for the basic physical and chemical theories of matter that are currently accepted do not preclude the kind of fusion here considered, and they do not imply that there would be a mass loss of the sort here referred to. Hence, even if the generalization *H* should be true, i.e., if no exceptions to it should ever occur, this would constitute a mere accident or coincidence as judged by current theory, which permits the occurrence of exceptions to *H*.

Thus, whether a statement of universal form counts as a law will depend in part upon the scientific theories accepted at the time. This

is not to say that "empirical generalizations"—statements of universal form that are empirically well confirmed but have no basis in theory—never qualify as laws: Galileo's, Kepler's, and Boyle's laws, for example, were accepted as such before they received theoretical grounding. The relevance of theory is rather this: a statement of universal form, whether empirically confirmed or as yet untested, will qualify as a law if it is implied by an accepted theory (statements of this kind are often referred to as theoretical laws); but even if it is empirically well confirmed and presumably true in fact, it will not qualify as a law if it rules out certain hypothetical occurrences (such as the fusion of two gold bodies with a resulting mass of more than 100,000 kilograms, in the case of our generalization *H*) which an accepted theory qualifies as possible.⁴

5.4 Probabilistic explanation: fundamentals

Not all scientific explanations are based on laws of strictly universal form. Thus, little Jim's getting the measles might be explained by saying that he caught the disease from his brother, who had a bad case of the measles some days earlier. This account again links the explanandum event to an earlier occurrence, Jim's exposure to the measles; the latter is said to provide an explanation because there is a connection between exposure to the measles and contracting the disease. That connection cannot be expressed by a law of universal form, however; for not every case of exposure to the measles produces contagion. What can be claimed is only that persons exposed to the measles will contract the disease with high probability, i.e., in a high percentage of all cases. General statements of this type, which we shall soon examine more closely, will be called *laws of probabilistic form* or *probabilistic laws*, for short.

In our illustration, then, the explanans consists of the probabilistic law just mentioned and the statement that Jim was exposed to the measles. In contrast to the case of deductive-nomological explanation, these explanans statements do not deductively imply the explanandum statement that Jim got the measles; for in deductive inferences from true premisses, the conclusion is invariably true, whereas in our example, it is clearly possible that the explanans statements might be true and yet the explanandum statement false. We will say, for short, that the explanans implies the explanandum, not with "deductive certainty", but only with near-certainty or with high probability.

The resulting explanatory argument may be schematized as follows at the top of page 59.

⁴ For a fuller analysis of the concept of law, and for further bibliographic references, see E. Nagel, *The Structure of Science* (New York: Harcourt, Brace & World, Inc., 1961), Chap. 4.

The probability for persons exposed to the measles to catch the disease is high.

Jim was exposed to the measles.

_____ [makes highly probable]
 Jim caught the measles.

In the customary presentation of a deductive argument, which was used, for example, in the schema (D-N) above, the conclusion is separated from the premisses by a single line, which serves to indicate that the premisses logically imply the conclusion. The double line used in our latest schema is meant to indicate analogously that the "premisses" (the explanans) make the "conclusion" (the explanandum sentence) more or less probable; the degree of probability is suggested by the notation in brackets.

Arguments of this kind will be called *probabilistic explanations*. As our discussion shows, a probabilistic explanation of a particular event shares certain basic characteristics with the corresponding deductive-nomological type of explanation. In both cases, the given event is explained by reference to others, with which the explanandum event is connected by laws. But in one case, the laws are of universal form; in the other, of probabilistic form. And while a deductive explanation shows that, on the information contained in the explanans, the explanandum was to be expected with "deductive certainty", an inductive explanation shows only that, on the information contained in the explanans, the explanandum was to be expected with high probability, and perhaps with "practical certainty"; it is in this manner that the latter argument meets the requirement of explanatory relevance.]

5.5 Statistical probabilities and probabilistic laws

We must now consider more closely the two differentiating features of probabilistic explanation that have just been noted: the probabilistic laws they invoke and the peculiar kind of probabilistic implication that connects the explanans with the explanandum.

Suppose that from an urn containing many balls of the same size and mass, but not necessarily of the same color, successive drawings are made. At each drawing, one ball is removed, and its color is noted. Then the ball is returned to the urn, whose contents are thoroughly mixed before the next drawing takes place. This is an example of a so-called random process or random experiment, a concept that will soon be characterized in more detail. Let us refer to the procedure just described as experiment *U*, to each drawing as one performance of *U*, and to the color of the ball produced by a given drawing as the result, or the outcome, of that performance.

If all the balls in an urn are white, then a statement of strictly universal form holds true of the results produced by the performance of

U: every drawing from the urn yields a white ball, or yields the result *W*, for short. If only some of the balls—say, 600 of them—are white, whereas the others—say 400—are red, then a general statement of probabilistic form holds true of the experiment: the probability for a performance of *U* to produce a white ball, or outcome *W*, is .6; in symbols:

$$5a) \quad P(W, U) = .6$$

Similarly, the probability of obtaining heads as a result of the random experiment *C* of flipping a fair coin is given by

$$5b) \quad P(H, C) = .5$$

and the probability of obtaining an ace as a result of the random experiment *D* of rolling a regular die is

$$5c) \quad P(A, D) = 1/6$$

What do such probability statements mean? According to one familiar view, sometimes called the "classical" conception of probability, the statement (5a) would have to be interpreted as follows: each performance of the experiment *U* effects a choice of one from among 1,000 basic possibilities, or basic alternatives, each represented by one of the balls in the urn; of these possible choices, 600 are "favorable" to the outcome *W*; and the probability of drawing a white ball is simply the ratio of the number of favorable choices available to the number of all possible choices, i.e., 600/1,000. The classical interpretation of the probability statements (5b) and (5c) follows similar lines.

Yet this characterization is inadequate; for if before each drawing, the 400 red balls in the urn were placed on top of the white ones, then in this new kind of urn experiment—let us call it *U'*—the ratio of favorable to possible basic alternatives would remain the same, but the probability of drawing a white ball would be smaller than in the experiment *U*, in which the balls are thoroughly mixed before each drawing. The classical conception takes account of this difficulty by requiring that the basic alternatives referred to in its definition of probability must be "equipossible" or "equiprobable"—a requirement presumably violated in the case of experiment *U'*.

This added proviso raises the question of how to define equipossibility or equiprobability. We will pass over this notoriously troublesome and controversial issue, because—even assuming that equiprobability can be satisfactorily characterized—the classical conception would still be inadequate, since probabilities are assigned also to the outcomes of random experiments for which no plausible way is known of marking off equiprobable basic alternatives. Thus, for the random experiment *D* of rolling a regular die, the six faces might be regarded as representing

such equiprobable alternatives; but we attribute probabilities to such results as rolling an ace, or an odd number of points, etc., also in the case of a loaded die, even though no equiprobable basic outcomes can be marked off here.

Similarly—and this is particularly important—science assigns probabilities to the outcomes of certain random experiments or random processes encountered in nature, such as the step-by-step decay of the atoms of radioactive substances, or the transition of atoms from one energy state to another. Here again, we find no equiprobable basic alternatives in terms of which such probabilities might be classically defined and computed.

To arrive at a more satisfactory construal of our probability statements, let us consider how one would ascertain the probability of the rolling of an ace with a given die that is not known to be regular. This would obviously be done by making a large number of throws with the die and ascertaining the *relative frequency*, i.e., the proportion, of those cases in which an ace turns up. If, for example, the experiment *D* of rolling the given die is performed 300 times and an ace turns up in 62 cases, then the relative frequency, 62/300, would be regarded as an approximate value of the probability $p(A, D')$ of rolling an ace with the given die. Analogous procedures would be used to estimate the probabilities associated with the flipping of a given coin, the spinning of a roulette wheel, and so on. Similarly, the probabilities associated with radioactive decay, with the transitions between different atomic energy states, with genetic processes, etc., are determined by ascertaining the corresponding relative frequencies; however, this is often done in highly indirect ways rather than by simply counting individual atomic or other events of the relevant kinds.

The interpretation in terms of relative frequencies applies also to probability statements such as (5b) and (5c), which concern the results of flipping a fair (i.e., homogeneous and strictly cylindrical) coin or tossing a regular (homogeneous and strictly cubical) die: what the scientist (or the gambler, for that matter) is concerned with in making a probability statement is the relative frequency with which a certain outcome *O* can be expected in long series of repetitions of some random experiment *R*. The counting of "equiprobable" basic alternatives and of those among them which are "favorable" to *O* may be regarded as a heuristic device for guessing at the relative frequency of *O*. And indeed when a regular die or a fair coin is tossed a large number of times, the different faces tend to come up with equal frequency. One might expect this on the basis of symmetry considerations of the kind frequently used in forming physical hypotheses, for our empirical knowledge affords no grounds on which to expect any of the faces to be favored over any

other. But while such considerations often are heuristically useful, they must not be regarded as certain or as self-evident truths: some very plausible symmetry assumptions, such as the principle of parity, have been found not to be generally satisfied at the subatomic level. Assumptions about equiprobabilities are therefore always subject to correction in the light of empirical data concerning the actual relative frequencies of the phenomena in question. This point is illustrated also by the statistical theories of gases developed by Bose and Einstein and by Fermi and Dirac, respectively, which rest on different assumptions concerning what distributions of particles over a phase space are equiprobable.

The probabilities specified in the probabilistic laws, then, represent relative frequencies. They cannot, however, be strictly defined as relative frequencies in long series of repetitions of the relevant random experiment. For the proportion, say, of aces obtained in throwing a given die will change, if perhaps only slightly, as the series of throws is extended; and even in two series of exactly the same length, the number of aces will usually differ. We do find, however, that as the number of throws increases, the relative frequency of each of the different outcomes tends to change less and less, even though the results of successive throws continue to vary in an irregular and practically unpredictable fashion. This is what generally characterizes a random experiment R with outcomes O_1, O_2, \dots, O_n : successive performances of R yield one or another of those outcomes in an irregular manner; but the relative frequencies of the outcomes tend to become stable as the number of performances increases. And the probabilities of the outcomes, $p(O_1, R), p(O_2, R), \dots, p(O_n, R)$, may be regarded as ideal values that the actual frequencies tend to assume as they become increasingly stable. For mathematical convenience, the probabilities are sometimes defined as the mathematical limits toward which the relative frequencies converge as the number of performances increases indefinitely. But this definition has certain conceptual shortcomings, and in some more recent mathematical studies of the subject, the intended empirical meaning of the concept of probability is deliberately, and for good reasons, characterized more vaguely by means of the following so-called *statistical interpretation of probability*:⁵

The statement

$$p(O, R) = r$$

means that in a long series of performances of random experiment R ,

⁵ Further details on the concept of statistical probability and on the limit-definition and its shortcomings will be found in E. Nagel's monograph, *Principles of the Theory of Probability* (Chicago: University of Chicago Press, 1939). Our version of the statistical interpretation follows that given by H. Cramér on pp. 148-49 of his book, *Mathematical Methods of Statistics* (Princeton: Princeton University Press, 1946).

the proportion of cases with outcome O is almost certain to be close to r .

The concept of *statistical probability* thus characterized must be carefully distinguished from the concept of *inductive or logical probability*, which we considered in section 4.5. Logical probability is a quantitative logical relation between definite statements; the sentence

$$c(H, K) = r$$

asserts that the hypothesis H is supported, or made probable, to degree r by the evidence formulated in statement K . Statistical probability is a quantitative relation between repeatable kinds of events: a certain kind of outcome, O , and a certain kind of random process, R ; it represents, roughly speaking, the relative frequency with which the result O tends to occur in a long series of performances of R .

What the two concepts have in common are their mathematical characteristics: both satisfy the basic principles of mathematical probability theory:

a] The possible numerical values of both probabilities range from 0 to 1:

$$\begin{aligned} 0 &\leq p(O, R) \leq 1 \\ 0 &\leq c(H, K) \leq 1 \end{aligned}$$

b] The probability for one of two mutually exclusive outcomes of R to occur is the sum of the probabilities of the outcomes taken separately; the probability, on any evidence K , for one or the other of two mutually exclusive hypotheses to hold is the sum of their respective probabilities:

If O_1, O_2 are mutually exclusive, then

$$p(O_1 \text{ or } O_2, R) = p(O_1, R) + p(O_2, R)$$

If H_1, H_2 are logically exclusive hypotheses, then

$$c(H_1 \text{ or } H_2, K) = c(H_1, K) + c(H_2, K)$$

c] The probability of an outcome that necessarily occurs in all cases—such as O or not O —is 1; the probability, on any evidence, of a hypothesis that is logically (and in this sense necessarily) true, such as H or not H , is 1:

$$\begin{aligned} p(O \text{ or not } O, R) &= 1 \\ c(H \text{ or not } H, K) &= 1 \end{aligned}$$

Scientific hypotheses in the form of statistical probability statements can be, and are, tested by examining the long-run relative frequencies of the outcomes concerned; and the confirmation of such hypotheses is then judged, broadly speaking, in terms of the closeness of the agreement between hypothetical probabilities and observed frequen-

cies. The logic of such tests, however, presents some intriguing special problems, which call for at least brief examination.

Consider the hypothesis, H , that the probability of rolling an ace with a certain die is .15; or briefly, that $p(A,D) = .15$, where D is the random experiment of rolling the given die. The hypothesis H does not deductively imply any test implications specifying how many aces will occur in a finite series of throws of the die. It does not imply, for example, that exactly 75 among the first 500 throws will yield an ace, nor even that the number of aces will lie between 50 and 100, say. Hence, if the proportion of aces actually obtained in a large number of throws differs considerably from .15, this does not refute H in the sense in which a hypothesis of strictly universal form, such as 'All swans are white', can be refuted, in virtue of the *modus tollens* argument, by reference to one counter-instance, such as a black swan. Similarly, if a long run of throws of the given die yields a proportion of aces very close to .15, this does not confirm H in the sense in which a hypothesis is confirmed by the finding that a test sentence I that it logically implies is in fact true. For in this latter case, the hypothesis asserts I by logical implication, and the test result is thus confirmatory in the sense of showing that a certain part of what the hypothesis asserts is indeed true; but nothing strictly analogous is shown for H by confirmatory frequency data; for H does not assert by implication that the frequency of aces in some long run will definitely be very close to .15.

But while H does not logically preclude the possibility that the proportion of aces obtained in a long series of throws of the given die may depart widely from .15, it does logically imply that such departures are highly improbable in the statistical sense; i.e., that if the experiment of performing a long series of throws (say, 1,000 of them per series) is repeated a large number of times, then only a tiny proportion of those long series will yield a proportion of aces that differs considerably from .15. For the case of rolling a die, it is usually assumed that the results of successive throws are "statistically independent"; this means roughly that the probability of obtaining an ace in a throw of the die does not depend on the result of the preceding throw. Mathematical analysis shows that in conjunction with this independence assumption, our hypothesis H deductively determines the statistical probability for the proportion of aces obtained in n throws to differ from .15 by no more than a specified amount. For example, H implies that for a series of 1,000 throws of the die here considered, the probability is about .976 that the proportion of aces will lie between .125 and .175; and similarly, that for a run of 10,000 throws the probability is about .995 that the proportion of aces will be between .14 and .16. Thus, we may say that if H is true, then it is practically certain that in a long trial run the

observed proportion of aces will differ by very little from the hypothetical probability value .15. Hence, if the observed long-run frequency of an outcome is not close to the probability assigned to it by a given probabilistic hypothesis, then that hypothesis is very likely to be false. In this case, the frequency data count as disconfirming the hypothesis, or as reducing its credibility; and if sufficiently strong disconfirming evidence is found, the hypothesis will be considered as practically, though not logically, refuted and will accordingly be rejected. Similarly, close agreement between hypothetical probabilities and observed frequencies will tend to confirm a probabilistic hypothesis and may lead to its acceptance.

If probabilistic hypotheses are to be accepted or rejected on the basis of statistical evidence concerning observed frequencies, then appropriate standards are called for. These will have to determine (a) what deviations of observed frequencies from the probability stated by a hypothesis are to count as grounds for rejecting the hypothesis, and (b) how close an agreement between observed frequencies and hypothetical probability is to be required as a condition for accepting the hypothesis. The requirements in question can be made more or less strict, and their specification is a matter of choice. The stringency of the chosen standards will normally vary with the context and the objectives of the research in question. Broadly speaking, it will depend on the importance that is attached, in the given context, to avoiding two kinds of error that might be made: rejecting the hypothesis under test although it is true, and accepting it although it is false. The importance of this point is particularly clear when acceptance or rejection of the hypothesis is to serve as a basis for practical action. Thus, if the hypothesis concerns the probable effectiveness and safety of a new vaccine, then the decision about its acceptance will have to take into account not only how well the statistical test results accord with the probabilities specified by the hypothesis, but also how serious would be the consequences of accepting the hypothesis and acting on it (e.g. by inoculating children with the vaccine) when in fact it is false, and of rejecting the hypothesis and acting accordingly (e.g. by destroying the vaccine and modifying or discontinuing the process of manufacture) when in fact the hypothesis is true. The complex problems that arise in this context form the subject matter of the theory of statistical tests and decisions, which has been developed in recent decades on the basis of the mathematical theory of probability and statistics.⁶

Many important laws and theoretical principles in the natural sciences are of probabilistic character, though they are often of more

⁶ On this subject, see R. D. Luce and H. Raiffa, *Games and Decisions* (New York: John Wiley & Sons, Inc., 1957).

complicated form than the simple probability statements we have discussed. For example, according to current physical theory, radioactive decay is a random phenomenon in which the atoms of each radioactive element possess a characteristic probability of disintegrating during a specified period of time. The corresponding probabilistic laws are usually formulated as statements giving the "half-life" of the element concerned. Thus, the statements that the half-life of radium²²⁶ is 1,620 years and that of polonium²¹⁸ is 3.05 minutes are laws to the effect that the probability for a radium²²⁶ atom to decay within 1,620 years, and for an atom of polonium²¹⁸ to decay within 3.05 minutes, are both one-half. According to the statistical interpretation cited earlier, these laws imply that of a large number of radium²²⁶ atoms or of polonium²¹⁸ atoms given at a certain time, very close to one-half will still exist 1,620 years, or 3.05 minutes, later; the others having disintegrated by radioactive decay.

Again, in the kinetic theory various uniformities in the behavior of gases, including the laws of classical thermodynamics, are explained by means of certain assumptions about the constituent molecules; and some of these are probabilistic hypotheses concerning statistical regularities in the motions and collisions of those molecules.

A few additional remarks concerning the notion of a probabilistic law are indicated. It might seem that all scientific laws should be qualified as probabilistic since the supporting evidence we have for them is always a finite and logically inconclusive body of findings, which can confer upon them only a more or less high probability. But this argument misses the point that the distinction between laws of universal form and laws of probabilistic form does not refer to the strength of the evidential support for the two kinds of statements, but to their form, which reflects the logical character of the claim they make. A law of universal form is basically a statement to the effect that in *all* cases where conditions of kind *F* are realized, conditions of kind *G* are realized as well; a law of probabilistic form asserts, basically, that under certain conditions, constituting the performance of a random experiment *R*, a certain kind of outcome will occur in a specified percentage of cases. No matter whether true or false, well supported or poorly supported, these two types of claims are of a logically different character, and it is on this difference that our distinction is based.

As we saw earlier, a law of the universal form "Whenever *F* then *G*" is by no means a brief, telescoped equivalent of a report stating for each occurrence of *F* so far examined that it was associated with an occurrence of *G*. Rather, it implies assertions also for all unexamined cases of *F*, past as well as present and future; also, it implies counterfactual and hypothetical conditionals which concern, so to speak "possible occurrences" of *F*; and it is just this characteristic that gives such

laws their explanatory power. Laws of probabilistic form have an analogous status. The law stating that the radioactive decay of radium²²⁶ is a random process with an associated half-life of 1,620 years is plainly not tantamount to a report about decay rates that have been observed in certain samples of radium²²⁶. It concerns the decaying process of any body of radium²²⁶—past, present, or future; and it implies subjunctive and counterfactual conditionals, such as: if two particular lumps of radium²²⁶ were to be combined into one, the decay rates would remain the same as if the lumps had remained separate. Again, it is this characteristic that gives probabilistic laws their predictive and their explanatory force.

One of the simplest kinds of probabilistic explanation is illustrated by our earlier example of Jim's catching the measles. The general form of that explanatory argument may be stated thus:

$p(0, R)$ is close to 1
i is a case of *R* [makes highly probable]

i is a case of 0

5.6 The
 inductive
 character of
 probabilistic
 explanation



Now the high probability which, as indicated in brackets, the explanans confers upon the explanandum is surely not a statistical probability, for it characterizes a relation between sentences, not between (kinds of) events. Using a term introduced in Chapter 4, we might say that the probability in question represents the rational credibility of the explanandum, given the information provided by the explanans; and as we noted earlier, in so far as this notion can be construed as a probability, it represents a logical or inductive probability.

In some simple cases, there is a natural and obvious way of expressing that probability in numerical terms. In an argument of the kind just considered, if the numerical value of $p(O, R)$ is specified, then it is reasonable to say that the inductive probability that the explanans confers upon the explanandum has the same numerical value. The resulting probabilistic explanation has the form:

$p(0, R) = r$
i is a case of *R* [*r*]

i is a case of 0

If the explanans is more complex, the determination of corresponding inductive probabilities for the explanandum raises difficult problems, which in part are still unsettled. But whether or not it is possible to assign definite numerical probabilities to all such explanations, the preceding considerations show that when an event is explained by reference

to probabilistic laws, the explanans confers upon the explanandum only more or less strong inductive support. Thus, we may distinguish deductive-nomological from probabilistic explanations by saying that the former effect a deductive subsumption under laws of universal form, the latter an inductive subsumption under laws of probabilistic form.

It is sometimes said that precisely because of its inductive character, a probabilistic account does not explain the occurrence of an event, since the explanans does not logically preclude its nonoccurrence. But the important, steadily expanding role that probabilistic laws and theories play in science and its applications, makes it preferable to view accounts based on such principles as affording explanations as well, though of a less stringent kind than those of deductive-nomological form. Take, for example, the radioactive decay of a sample of one milligram of polonium²¹⁸. Suppose that what is left of this initial amount after 3.05 minutes is found to have a mass that falls within the interval from .499 to .501 milligrams. This finding can be explained by the probabilistic law of decay for polonium²¹⁸; for that law, in combination with the principles of mathematical probability, deductively implies that given the huge number of atoms in a milligram of polonium²¹⁸, the probability of the specified outcome is overwhelmingly large, so that in a particular case its occurrence may be expected with "practical certainty".

Or consider the explanation offered by the kinetic theory of gases for an empirically established generalization called Graham's law of diffusion. The law states that at fixed temperature and pressure, the rates at which different gases in a container escape, or diffuse, through a thin porous wall are inversely proportional to the square roots of their molecular weights; so that the amount of a gas that diffuses through the wall per second will be the greater, the lighter its molecules. The explanation rests on the consideration that the mass of a given gas that diffuses through the wall per second will be proportional to the average velocity of its molecules, and that Graham's law will therefore have been explained if it can be shown that the average molecular velocities of different pure gases are inversely proportional to the square roots of their molecular weights. To show this, the theory makes certain assumptions broadly to the effect that a gas consists of a very large number of molecules moving in random fashion at different speeds that frequently change as a result of collisions, and that this random behavior shows certain probabilistic uniformities—in particular, that among the molecules of a given gas at specified temperature and pressure, different velocities will occur with definite, and different, probabilities. These assumptions make it possible to compute the probabilistically expected values—or, as we might briefly say, the "most probable" values—that the average velocities of different gases will possess at equal temperatures and

pressures. These most probable average values, the theory shows, are indeed inversely proportional to the square roots of the molecular weights of the gases. But the actual diffusion rates, which are measured experimentally and are the subject of Graham's law, will depend on the actual values that the average velocities have in the large but finite swarms of molecules constituting the given bodies of gas. And the actual average values are related to the corresponding probabilistically estimated, or "most probable", values in a manner that is basically analogous to the relation between the proportion of aces occurring in a large but finite series of tossings of a given die and the corresponding probability of rolling an ace with that die. From the theoretically derived conclusion concerning the probabilistic estimates, it follows only that in view of the very large number of molecules involved, it is overwhelmingly probable that at any given time the actual average speeds will have values very close to their probability estimates and that, therefore, it is *practically certain* that they will be, like the latter, inversely proportional to the square roots of their molecular masses, thus satisfying Graham's law.⁷

It seems reasonable to say that this account affords an explanation, even though "only" with very high associated probability, of why gases display the uniformity expressed by Graham's law; and in physical texts and treatises, theoretical accounts of this probabilistic kind are indeed very widely referred to as explanations.

⁷ The "average" velocities here referred to are technically defined as root-mean-square velocities. Their values do not differ very much from those of average velocities in the usual sense of the arithmetic mean. A succinct outline of the theoretical explanation of Graham's law can be found in Chap. 25 of Holton and Roller, *Foundations of Modern Physical Science*. The distinction, not explicitly mentioned in that presentation, between the average value of a quantity for some finite number of cases and the probabilistically estimated or expected value of that quantity is briefly discussed in Chap. 6 (especially section 4) of R. P. Feynman, R. B. Leighton, and M. Sands, *The Feynman Lectures on Physics* (Reading, Mass.: Addison-Wesley Publishing Co., 1963).

8

**8.1 The
mechanism-
vitalism
issue**

We considered earlier the neovitalistic doctrine that certain characteristics of living systems—among them their adaptive and self-regulating features—cannot be explained by physical and chemical principles alone, but have to be accounted for by reference to new factors, of a kind not known in the physical sciences, namely entelechies or vital forces. Closer consideration showed that the concept of entelechy as used by neovitalists cannot possibly provide an explanation of any biological phenomenon. The reasons that led us to this conclusion do not, however, automatically dispose of the basic neovitalistic idea that biological systems and processes differ in certain fundamental respects from purely physico-chemical ones. This view is opposed by the so-called mechanistic claim that living organisms are nothing else than very complex physico-chemical systems (though not, as the old-fashioned term 'mechanism' would suggest, purely mechanical ones). These conflicting conceptions have been the subject of an extensive and heated debate, whose details we cannot consider here. But evidently, the issue can be fruitfully discussed only if the meaning of the opposing claims can be made sufficiently clear to show what sorts of argument and evidence can have a bearing on the problem and how the controversy might be settled. It is this characteristically philosophical problem of clarifying the meanings of the conflicting conceptions that we shall now consider; the result of our reflections will also have certain implications concerning the possibility of settling the issue.

Ostensibly, the controversy concerns the question whether or not living organisms are "merely", or exclusively, physico-chemical systems. But just what would it mean to say that they are? Our introductory

remarks suggest that we might construe the doctrine of mechanism as making this twofold claim: (M_1) all the characteristics of living organisms are physico-chemical characteristics—they can be fully described in terms of the concepts of physics and chemistry; (M_2) all aspects of the behavior of living organisms that can be explained at all can be explained by means of physico-chemical laws and theories.

As for the first of these assertions, it is clear that at present, at any rate, the description of biological phenomena requires the use not only of physical and chemical terms, but of specifically biological terms that do not occur in the physico-chemical vocabulary. Take the statement that in the first stage of mitosis, there occurs, among other things, a contraction of the chromosomes in the nucleus of the dividing cell; or take the much less technical statement that a fertilized goose egg, when properly hatched, will yield a gosling. Thesis M_1 implies that the biological entities and processes here referred to—goslings, goose eggs, cells, nuclei, chromosomes, fertilization, and mitosis—can all be fully characterized in physico-chemical terms. The most plausible construal of this claim is that the corresponding biological terms, 'gosling', 'cell', etc., can be defined with the help of terms taken from the vocabulary of physics and chemistry. Let us refer to this more specific version of M_1 as M_1' . Similarly, if all biological phenomena—and thus, in particular, all the uniformities expressed by biological laws—are to be explainable by means of physico-chemical principles, then all the laws of biology will have to be derivable from the laws and theoretical principles of physics and chemistry. The thesis—let us call it M_2' —that this is indeed the case may be regarded as a more specific version of M_2 .

Jointly, the statements M_1' and M_2' express what is often called the thesis of *reducibility of biology to physics and chemistry*. This thesis concerns both the concepts and the laws of the disciplines concerned: reducibility of the concepts of one discipline to those of another is construed as definability of the former in terms of the latter; reducibility of the laws is analogously construed as derivability. Mechanism may thus be said to assert the reducibility of biology to physics and chemistry. The denial of this claim is sometimes referred to as the thesis of the *autonomy of biology* or, better, of biological concepts and principles. Neovitalism thus affirms the autonomy of biology and supplements this claim with its doctrine of vital forces. Let us now consider the mechanistic theses in more detail.

8.2 Reduction of terms

The thesis M_1' , concerning the definability of biological terms is not meant, of course, to assert the possibility of assigning physico-chemical meanings to biological terms by arbitrary stipulative definitions. It takes for granted that the terms in the vocabulary of

biology have definite technical meanings but claims that, in a sense we must try to clarify, their import can be adequately expressed with the help of physical and chemical concepts. The thesis, then, affirms the possibility of giving what, in Chapter 7, we broadly called "descriptive definitions" of biological concepts in physico-chemical terms. But the definitions in question could hardly be expected to be analytic. For it would obviously be false to claim that for every biological term—for example, 'goose egg', 'retina', 'mitosis', 'virus', 'hormone'—there exists an expression in physico-chemical terms that has the same meaning in the sense in which 'spouse' may be said to have the same meaning as, or to be synonymous with, 'husband or wife'. It would be very difficult to name even one biological term for which a physico-chemical synonym can be specified; and it would be preposterous to saddle mechanism with this construal of its claim. But descriptive definition may also be understood in a less stringent sense, which does not require that the definiens have the same meaning, or intension, as the definiendum, but only that it have the same extension or application. The definiens in this case specifies conditions that, as a matter of fact, are satisfied by all and only those instances to which the definiendum applies. A traditional example is the definition of 'man' by 'featherless biped'; it does not assert that the word 'man' has the same meaning as the expression 'featherless biped', but only that it has the same extension, that the term 'man' applies to all and only those things that are featherless bipeds, or that being a featherless biped is both a necessary and a sufficient condition for being a man. Statements of this kind might be referred to as *extensional definitions*; they can be schematically expressed in the form

— has the same extension as — — —

The definitions to which a mechanist might point to illustrate and support his claim concerning biological concepts are of this extensional type: they express necessary and sufficient physico-chemical conditions for the applicability of biological terms, and they are therefore the results of often very difficult biophysical or biochemical research. This is illustrated by the characterization of substances such as penicillin, testosterone, and cholesterol in terms of their molecular structures—an achievement that permits the "definition" of the biological terms by means of purely chemical ones. But such definitions do not purport to express the meanings of the biological terms. The original meaning of the word 'penicillin', for example, would have to be indicated by characterizing penicillin as an antibacterial substance produced by the fungus *penicillium notatum*; testosterone is originally defined as a male sex hormone, produced by the testes; and so forth. The characterization of these substances by their molecular structure is arrived at, not by mean-

ing analysis, but by chemical analysis; the result constitutes a biochemical discovery, not a logical or philosophical one; it is expressed by empirical laws, not by statements of synonymy. In fact, acceptance of the chemical characterizations as new definitions of the biological terms involves a change not only in meaning or intension, but also in extension. For the chemical criteria qualify as penicillin or as testosterone certain substances that were not produced by organic systems, but were synthesized in a laboratory.

At any rate, however, the establishment of such definitions requires empirical research. We must conclude therefore that, in general, the question whether a biological term is "definable" by means of physical and chemical terms alone cannot be settled by just contemplating its meaning, nor by any other nonempirical procedure. Hence, the thesis M'_1 cannot be established or refuted on *a priori* grounds, i.e., by considerations that can be developed "prior to"—or better, independently of—empirical evidence.

8.3 Reduction of laws

We turn now to the second thesis, M'_2 , in our construal of mechanism—the thesis asserting that the laws and theoretical principles of biology are derivable from those of physics and chemistry. It is clear that logical deductions from statements couched exclusively in physical and chemical terms will not yield characteristically biological laws, since these have to contain also specifically biological terms.¹ To obtain such laws, we will need some additional premises that express connections between physico-chemical characteristics and biological ones. The logical situation here is the same as in the explanatory use of a theory, where bridge principles are required, in addition to internal theoretical principles, for the derivation of consequences that can be expressed exclusively in pretheoretical terms. The additional premises required for the deduction of biological laws from physico-chemical ones would have to contain both biological and physico-chemical terms and would have the character of laws connecting certain physico-chemical

¹ It might seem obvious that the consequences logically deducible from a set of premises cannot contain any "new" terms, i.e., terms that do not occur in the premises. But this is not so. The physical statement 'When a gas is heated under constant pressure, it expands' logically implies 'When a gas is heated under constant pressure, it expands or turns into a swarm of mosquitoes'. In this manner, then, biological statements are deducible from physical ones alone. But the same physical premises also permits the deduction of the statements 'When a gas is heated under constant pressure, it expands or does not turn into a swarm of mosquitoes'; 'When a gas heated under constant pressure, it expands or turns into a rabbit', and so on. Generally, any biological statement that can be deduced from the given physical law has this peculiarity: if the specifically biological terms occurring in it are replaced by their negatives or by any other terms, the sentence thus obtained is equally deducible from the physical law. In this sense, the physical law fails to offer an explanation for any specific biological phenomenon.

aspects of a phenomenon with certain biological ones. A connective statement of this kind might take the special form of the laws we have just considered, which afford a basis for an extensional definition of biological terms. Such a statement asserts, in effect, that the presence of certain physico-chemical characteristics (e.g., a substance being of such and such a molecular structure) is both necessary and sufficient for the presence of a certain biological characteristic (e.g., being testosterone). Other connective statements might express physico-chemical conditions that are necessary but not sufficient, or conditions that are sufficient but not necessary, for a given biological characteristic. The generalizations 'where there is vertebrate life there is oxygen' and 'any nerve fiber conducts electric impulses' are of the former kind; the statement that the nerve gas tabun (characterized by its molecular structure) blocks nervous activity and thus causes death in man is of the second kind. Connective statements of various other types are also conceivable.

One very simple form that the derivation of a biological law from a physico-chemical one might take can be schematically described as follows: Let ' P_1 ', ' P_2 ' be expressions containing only physico-chemical terms, and let ' B_1 ', ' B_2 ' be expressions containing one or more specifically biological terms (and possibly physico-chemical ones as well). Let the statement 'all cases of P_1 are cases of P_2 ' be a physico-chemical law—we will call it L_P —and let the following connecting laws be given: 'All cases of B_1 are cases of P_1 ' and 'All cases of P_2 are cases of B_2 ' (the first states that physico-chemical conditions of kind P_1 are necessary for the occurrence of the biological state or condition B_1 ; the second, that physico-chemical conditions P_2 are sufficient for biological feature B_2). Then, as is readily seen, a purely biological law can be logically deduced from the physico-chemical law L_P in conjunction with the connecting laws; namely, 'all cases of B_1 are cases of B_2 ' (or: 'Whenever the biological features B_1 occur then so do the biological features B_2 ').

Generally, then, the extent to which biological laws are explainable by means of physico-chemical laws depends on the extent to which suitable connecting laws can be established. And that, again, cannot be decided by *a priori* arguments; the answer can be found only by biological and biophysical research.

8.4 Mechanism restated

The physical and chemical theories and the connecting laws available at present certainly do not suffice to reduce the terms and laws of biology to those of physics and chemistry. But research in the field is rapidly advancing and is steadily expanding the reach of a physico-chemical interpretation of biological phenomena. One might therefore construe mechanism as the view that in the course of further scientific research, biology will eventually come to be reduced to physics

and chemistry. But this formulation calls for a word of caution. In our discussion, we have assumed that a clear distinction can be drawn between the terms of physics and chemistry on one hand and specifically biological terms on the other. And indeed, if we were presented with any scientific term currently in use, we would probably not find it difficult to decide in an intuitive fashion whether it belonged to one or to the other of those vocabularies or to neither. But it would be very difficult to formulate explicit general criteria by means of which any scientific term now in use, and also any term that might be introduced in the future, could be unequivocally assigned to the specific vocabulary of one particular discipline. Indeed, it may be impossible to give such criteria. For in the course of future research, the dividing line between biology and physics-and-chemistry may become as blurred as that between physics and chemistry has become in our time. Future theories might well be couched in novel kinds of terms functioning in comprehensive theories that afford explanations both for phenomena now called biological and for others now called physical or chemical. To the vocabulary of such a comprehensive unifying theory, the division into physical-chemical terms and biological terms might no longer be significantly applicable, and the notion of eventually reducing biology to physics and chemistry would lose its meaning.

Such a theoretical development, however, is not at hand as yet; and in the meantime, mechanism is perhaps best construed, not as a specific thesis or theory about the character of biological processes, but as a heuristic maxim, as a principle for the guidance of research. Thus understood, it enjoins the scientist to persist in the search for basic physico-chemical theories of biological phenomena rather than resign himself to the view that the concepts and principles of physics and chemistry are powerless to give an adequate account of the phenomena of life. Adherence to this maxim has certainly proved very successful in biophysical and biochemical research—a credential that cannot be matched by the vitalistic view of life.

8.5 Reduction of psychology; behaviorism

The question of reducibility has been raised also for scientific disciplines other than biology. It is of particular interest in the case of psychology, where it has a direct bearing on the famous psycho-physical problem, i.e., the question of the relationship between mind and body. A reductionist view concerning psychology holds, roughly speaking, that all psychological phenomena are basically biological or physico-chemical in character; or more precisely, that the specific terms and laws of psychology can be reduced to those of biology, chemistry, and physics. Reduction is here to be understood in the sense defined earlier, and our general comments on the subject apply also to

the case of psychology. Thus, the reductive "definition" of a psychological term would require the specification of biological or physico-chemical conditions that are both necessary and sufficient for the occurrence of the mental characteristic, state, or process (such as, intelligence, hunger, hallucination, dreaming) for which the term stands. And the reduction of psychological laws would require suitable connecting principles containing psychological terms as well as biological or physico-chemical ones.

Some such connecting principles, expressing sufficient or necessary conditions for certain psychological states are indeed available: depriving an individual of food or drink or opportunity for rest is sufficient for the occurrence of hunger, thirst, fatigue; the administration of certain drugs is perhaps sufficient for the occurrence of hallucinations; the presence of certain nerve connections is necessary for the occurrence of certain sensations and for visual perception; proper oxygen supply to the brain is necessary for mental activity and indeed for consciousness.

One especially important class of biological or physical indicators of psychological states and events consists in the publicly observable behavior of the individual to whom those states or events are ascribed. Such behavior may be understood to include both large-scale, directly observable manifestations, such as body movements, facial expressions, blushing, verbal utterances, performance of certain tasks (as in psychological tests), and subtler responses such as changes in blood pressure and heartbeat, skin conductivity, and blood chemistry. Thus, fatigue may manifest itself in speech utterances ("I feel tired", etc.), in a decreasing rate and quality of performance at certain tasks, in yawning, and in physiological changes; certain affective and emotional processes are accompanied by changes in apparent skin resistance, as measured by "lie detectors"; the preferences and values a person holds express themselves in the way he responds when offered certain relevant choices; his beliefs, in verbal utterances that may be elicited from him, and also in the ways he acts—for example, a driver's belief that a road is closed may show itself in his taking a detour.

Certain characteristic kinds of "overt" (publicly observable) behavior that a subject in a given psychological state, or with a given psychological property, tends to manifest in appropriate "stimulus" or "test" situations are widely used in psychology as operational criteria for the presence of the psychological state or property in question. For intelligence or for introversion, the test situation might consist in presenting the subject with appropriate questionnaires; the response, in the answers the subject produces. The intensity of an animal's hunger drive will manifest itself in such behavioral features as salivation, the strength of the electric shock that the animal will take to reach food, or the

amount of food it consumes. To the extent that the stimuli and the responses can be described in biological or physico-chemical terms, the resulting criteria may be said to afford partial specifications of meaning for psychological expressions in terms of the vocabularies of biology, chemistry, and physics. Though they are often referred to as operational definitions, they do not actually determine necessary and sufficient conditions for the psychological terms: the logical situation is quite similar to the one we encountered in examining the relation of biological terms to the physical and chemical vocabulary.

Behaviorism is an influential school of thought in psychology which, in all its different forms, has a basically reductionist orientation; in a more or less strict sense, it seeks to reduce discourse about psychological phenomena to discourse about behavioral phenomena. One form of behaviorism, which is especially concerned to ensure the objective public testability of psychological hypotheses and theories, insists that all psychological terms must have clearly specified criteria of application couched in behavioral terms, and that psychological hypotheses and theories must have test implications concerning publicly observable behavior. This school of thought rejects, in particular, all reliance on methods such as introspection, which can be used only by the subject himself in a phenomenological exploration of his mental world; it does not admit as psychological data any of the "private" psychological phenomena—such as sensations, feelings, hopes, and fears—that introspective methods are said to reveal.

While behaviorists are agreed in their insistence on objective behavioral criteria for psychological characteristics, states, and events, they differ (or are noncommittal) on the question whether or not psychological phenomena are distinct from the corresponding, often very subtle and complex, behavioral phenomena—whether the latter are only their public manifestations, or whether psychological phenomena are, in some clear sense, identical with certain complex behavioral properties, states, or events. One recent version of behaviorism, which has exerted a strong influence on the philosophical analysis of psychological concepts, holds that psychological terms, though ostensibly referring to mental states and to processes "in the mind", serve, in effect, simply as a means of speaking about more or less intricate aspects of behavior—specifically, about propensities or dispositions to behave in characteristic ways in certain situations. On this view, to say of a person that he is intelligent is to say that he tends to act, or has a disposition to act, in certain characteristic ways; namely, in ways that we would normally qualify as intelligent action under the circumstances. To say of someone that he speaks Russian is not to say, of course, that he constantly utters Russian expressions, but that he is capable of a specific kind of behavior that

shows itself in particular situations and that is generally considered characteristic of a person who understands and speaks Russian. Thinking of Vienna, being fond of jazz, being honest, being forgetful, seeing certain things, having certain wants can all be viewed in a similar way. And viewing them in this manner—so this form of behaviorism holds—disposes of the baffling aspect of the mind-body problem: there is then no point any more to searching for the "ghost in the machine";² for the mental entities and processes that go on "behind" the physical façade. Consider an analogy. Of a watch that keeps time very well we say that it has a very high accuracy; to ascribe high accuracy to it is tantamount to saying that it tends to keep time well. It makes no sense, therefore, to ask in what manner that nonsubstantial agency, the accuracy, acts upon the mechanism of the clock; nor does it make sense to ask what happens to the accuracy when the clock stops running. Similarly, on this version of behaviorism, it makes no sense to ask how mental events or characteristics affect the behavior of an organism.

This conception, which has contributed greatly to clarifying the role of psychological concepts, is evidently reductionist in tenor; it presents the concepts of psychology as affording an effective and convenient way of speaking about subtle patterns of behavior. The supporting arguments, however, do not establish that all the concepts of psychology are actually *definable* in terms of nonpsychological concepts of the kind required to describe overt behavior and behavioral dispositions; and this for at least two reasons. First, it is very doubtful that all the different kinds of situation in which a person could "act intelligently" (for example), and the particular kinds of action that would qualify as intelligent in each of those situations, could be encompassed in a clear-cut, fully explicit definition. Second, it seems that the circumstances under which, and the manner in which, intelligence or courage or spitefulness can manifest themselves in overt behavior cannot be adequately stated in terms of a "purely behavioristic vocabulary", which might contain biological, chemical, and physical terms as well as nontechnical expressions of our everyday language, such as 'shaking one's head', 'stretching out one's hand', 'wincing', 'grimacing', 'laughing', and the like: it seems that psychological terms are needed as well to characterize the kinds of behavior patterns, or behavioral dispositions and capacities, that such terms as 'tired', 'intelligent', 'knows Russian' presumably indicate. For whether an agent's overt behavior in a given situation qualifies as intelligent, courageous, foolhardy, courteous, rude, etc., will not simply

² This phrase was coined by Gilbert Ryle, whose stimulating and influential book, *The Concept of Mind* (London: Hutchinson, 1949) develops in detail a conception of psychological phenomena and psychological locutions that is behavioristic in the sense here briefly sketched.

depend on what the facts of the situation are, but very importantly on what the agent knows or believes about the situation in which he finds himself. A man who walks unflinchingly toward a thicket where a hungry lion is crouching is not acting courageously if he does not believe (and hence does not know) that there is a lion in the thicket. Similarly, whether a person's behavior in a given situation qualifies as intelligent will depend on what he *believes* about the situation and what objectives he *wants* to attain by his action. Thus, it appears that in order to characterize the behavioral patterns, propensities, or capacities to which psychological terms refer, we need not only a suitable behavioristic vocabulary, but psychological terms as well. This consideration does not prove, of course, that a reduction of psychological terms to a behavioristic vocabulary is impossible, but it does remind us that the possibility of such a reduction has not been established by the kind of analysis we have considered.

Another discipline to which it has been thought that psychology might eventually be reduced is that of physiology, and especially neurophysiology; but again, a full reduction in the sense we specified earlier is not remotely in sight.

Questions of reducibility arise also with respect to the social sciences, particularly in connection with the doctrine of methodological individualism,³ according to which all social phenomena should be described, analyzed, and explained in terms of the situations of the individual agents involved in them and by reference to the laws and theories concerning individual behavior. The description of an agent's "situation" would have to take into account his motives and beliefs as well as his physiological state and various biological, chemical, and physical factors in his environment. The doctrine of methodological individualism may therefore be viewed as implying the reducibility of the specific concepts and laws of the social sciences (in a broad sense, including group psychology, the theory of economic behavior, and the like) to those of individual psychology, biology, chemistry, and physics. The problems raised by this claim fall outside the scope of this book. They belong to the philosophy of the social sciences and have been mentioned here simply as a further illustration of the problem of theoretical reducibility and as an example of the many logical and methodological affinities between the natural and the social sciences.

³ A lucid discussion of this doctrine can be found in E. Nagel, *The Structure of Science*, pp. 535-46.

For further reading

The list below includes only a few selected works, most of which provide, however, extensive further references to the literature in the field.

Anthologies

- A. Danto and S. Morgenbesser, eds., *Philosophy of Science*. New York: Meridian Books, 1960. (Paperback.)
 H. Feigl and M. Brodbeck, eds., *Readings in the Philosophy of Science*. New York: Appleton-Century-Crofts, 1953.
 E. H. Madden, ed., *The Structure of Scientific Thought*. Boston: Houghton Mifflin Company, 1960.
 P. P. Wiener, ed., *Readings in Philosophy of Science*. New York: Charles Scribner's Sons, 1953.

Works by individual authors

- N. Campbell, *What Is Science?* New York: Dover Publications, 1952. (Paperback.) A lucid introductory account of laws, theories, explanation, and measurement.
 R. Carnap, *Philosophical Foundations of Physics*, ed. Martin Gardner. New York, London: Basic Books, Inc., 1966. A fascinating introduction to a wide range of topics in the philosophy of physics, by one of the most eminent contemporary logicians and philosophers of science.
 P. Caws, *The Philosophy of Science*. Princeton: D. Van Nostrand Co., 1965. A clear introductory discussion of the main logical, methodological, and philosophical aspects of scientific theorizing.
 A. Grünbaum, *Philosophical Problems of Space and Time*. New York: Alfred A. Knopf, 1963. A very substantial, carefully probing, advanced work